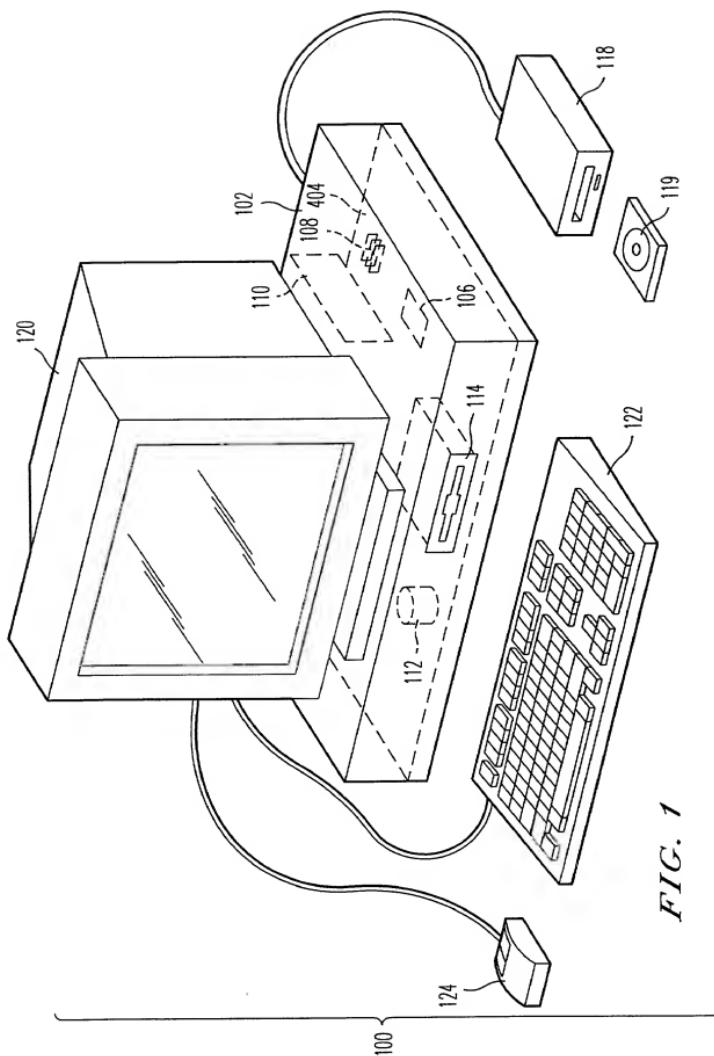


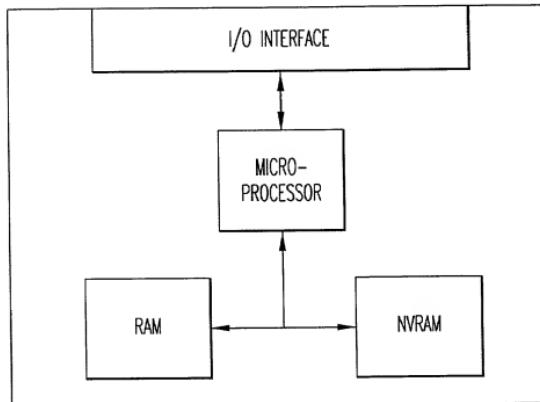
*FIG. 1*



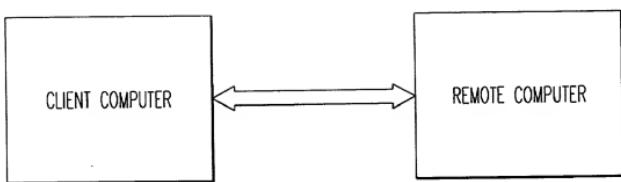
DEBIT CARD



*FIG. 2*

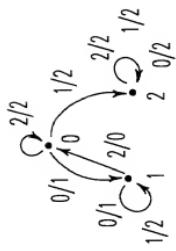


*FIG. 3*

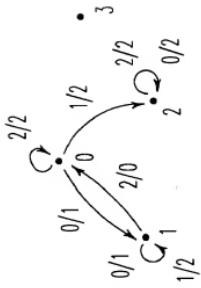


*FIG. 4*

09737742.121800



*FIG. 5A*



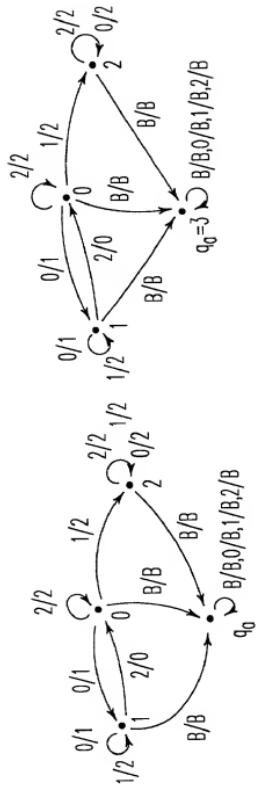
*FIG. 5C*

STATE \ INPUT	0	1	2
0	(1,1)	(2,2)	(0,2)
1	(1,1)	(1,2)	(0,0)
2	(2,2)	(2,2)	—

*FIG. 5B*

STATE \ INPUT	0	1	2
0	(1,1)	(2,2)	(0,2)
1	(1,1)	(1,2)	(0,0)
2	(2,2)	—	(2,2)

*FIG. 5D*



*FIG. 6A*

*FIG. 6C*

CORRESPONDING FUNCTION TABLE

INPUT STATE	0	1	2	B
0	(1,1)	(2,2)	(0,2)	(q <sub>0</sub> ,B)
1	(1,1)	(1,2)	(0,0)	(q <sub>0</sub> ,B)
2	(2,2)	(2,2)	(2,2)	(q <sub>0</sub> ,B)
q <sub>0</sub>	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)

CORRESPONDING FUNCTION TABLE

INPUT STATE	0	1	2	B
0	(1,1)	(2,2)	(2,2)	(1,0)
1	(1,1)	(1,2)	(1,2)	(0,0)
2	(2,2)	(2,2)	(2,2)	(2,2)
q <sub>0</sub>	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)	(q <sub>0</sub> ,B)

*FIG. 6B*

*FIG. 6D*

INPUT SPACE:  $\Sigma' = \{0,1,2,B\}$   
 STATE SPACE:  $Q' = \{0,1,2,q_0\}$ ,  $q_0=3$   
 OUTPUT SPACE:  $\Delta' = \{0,1,2,3\}$

VECTORIZATION EXAMPLE FOR N=2:

$\begin{matrix} 0 & 1 & 2 & B \\ \hline 0 & (0,0) & (0,1) & (1,0) & (1,1) \end{matrix}$   
 INPUT SPACE:  $\Sigma' = \{(0,0), (0,1), (1,0), (1,1)\}$   
 $\begin{matrix} 0 & 1 & 2 & q_0=3 \\ \hline 0 & (0,0) & (0,1) & (1,0) & (1,1) \end{matrix}$   
 STATE SPACE:  $Q' = \{(0,0), (0,1), (1,0), (1,1)\}$   
 $\begin{matrix} 0 & 1 & 2 & 3 \\ \hline 0 & (0,0) & (0,1) & (1,0) & (1,1) \end{matrix}$   
 OUTPUT SPACE:  $\Delta' = \{(0,0), (0,1), (1,0), (1,1)\}$

FIG. 7A

VECTORIZATION EXAMPLE FOR N=3:

$\begin{matrix} 0 & 1 & 2 & B \\ \hline 0 & (0,0) & (0,1) & (0,2) & (1,0) \end{matrix}$   
 INPUT SPACE:  $\Sigma' = \{(0,0), (0,1), (0,2), (1,0)\}$   
 $\begin{matrix} 0 & 1 & 2 & q_0=3 \\ \hline 0 & (0,0) & (0,1) & (0,2) & (1,0) \end{matrix}$   
 STATE SPACE:  $Q' = \{(0,0), (0,1), (0,2), (1,0)\}$   
 $\begin{matrix} 0 & 1 & 2 & B \\ \hline 0 & (0,0) & (0,1) & (0,2) & (1,0) \end{matrix}$   
 OUTPUT SPACE:  $\Delta' = \{(0,0), (0,1), (0,2), (1,0)\}$

FIG. 7B

VECTORIZATION EXAMPLE FOR  $N \geq 4$

$\begin{matrix} 0 & 1 & 2 & B \\ \hline 0 & (0) & (1) & (2) & (3) \end{matrix}$   
 INPUT SPACE:  $\Sigma' = \{(0), (1), (2), (3)\}$   
 $\begin{matrix} 0 & 1 & 2 & q_0=3 \\ \hline 0 & (0) & (1) & (2) & (3) \end{matrix}$   
 STATE SPACE:  $Q' = \{(0), (1), (2), (3)\}$   
 $\begin{matrix} 0 & 1 & 2 \\ \hline 0 & (0) & (1) & (2) & (3) \end{matrix}$   
 OUTPUT SPACE:  $\Delta' = \{(0), (1), (2), (3)\}$

FIG. 7C

VECTORIZATION EXAMPLE FOR  $N'=2$ :

INPUT SPACE:  $\Sigma' = \{(0,0), (0,1), (1,0), (1,1)\}$

STATE SPACE:  $Q' = \{(0,0), (0,1), (1,0), (1,1)\}$

OUTPUT:  $\Delta' = \{(0,0), (0,1), (1,0), (1,1)\}$

IN THIS CASE N MAY BE SET TO ANY PRIME NUMBER  $\geq 2$ .

SELECTING PRIMES  $N > 2$  RESULTS IN  $(N-2)^2$  INPUT, STATE AND OUTPUT REPRESENTATIONS THAT INITIALLY REMAIN UNUSED.

### *FIG. 8A*

VECTORIZATION EXAMPLE FOR  $N'=3$ :

INPUT SPACE:  $\Sigma' = \{(0,0), (0,1), (0,2), (1,0)\}$

STATE SPACE:  $Q' = \{(0,0), (0,1), (0,2), (1,0)\}$

OUTPUT:  $\Delta' = \{(0,0), (0,1), (0,2), (1,0)\}$

IN THIS CASE N MAY BE SET TO ANY PRIME NUMBER  $\geq 3$ .

FOR EVERY N THERE ARE  $N^2 - 4$  UNUSED REPRESENTATIONS FOR INPUT VECTORS (INPUT "SYMBOLS"), STATE VECTORS, AND OUTPUT VECTORS (OUTPUT "SYMBOLS").

### *FIG. 8B*

VECTORIZATION EXAMPLE FOR  $N' \geq 4$ :

INPUT SPACE:  $\Sigma' = \{(0), (1), (2), (3)\}$

STATE SPACE:  $Q' = \{(0), (1), (2), (3)\}$

OUTPUT:  $\Delta' = \{(0), (1), (2), (3)\}$

IN THIS CASE N MAY BE SET TO ANY PRIME NUMBER  $\geq 5$

FOR EVERY N THERE ARE  $N-4$  UNUSED REPRESENTATIONS FOR INPUT VECTORS, STATE VECTORS, AND OUTPUT VECTORS.

SELECTING AN N SUCH THAT THERE ARE MORE VALUES FOR N THAN OUTPUT VECTORS, INPUT VECTORS OR STATES IS SOMETHING THAT CAN BE DONE TO INCREASE THE POSSIBILITIES FOR INTRODUCING RANDOMNESS INTO THE PLAINTEXT STATES MACHINE

### *FIG. 8C*

		(0,0)	(0,1)	(0,2)	(1,0)
		(0,0)	(0,1)	(0,2)	(1,0)
		(0,1)	(0,2)	(0,0)	(1,0)
$q_0 = 3$	(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
	(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
	(0,2)	((0,2),(0,2))	-----	((0,2),(0,2))	((1,0),(1,0))
	(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
	(1,1)	-----	-----	-----	-----
	(1,2)	-----	-----	-----	-----
	(2,0)	-----	-----	-----	-----
	(2,1)	-----	-----	-----	-----
	(2,2)	-----	-----	-----	-----

FIG. 9A

INPUT STATE	(0,0)	(0,1)	(0,2)	(1,0)	(1,1)	(1,2)	(2,0)	(2,1)	(2,2)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	((1,0),(1,0))	((0,2),(0,2))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,2)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(2,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(2,1)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(2,2)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))

FIG. 9B

INPUT STATE	(0,0)	(0,1)	(0,2)	(1,0)	(1,1)	(1,2)	(2,0)	(2,1)	(2,2)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(0,2)	((0,2),(0,2))	((0,2),(0,1))	((0,2),(0,2))	((1,0),(1,0))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(1,1)	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(1,2)	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(2,0)	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(2,1)	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))
(2,2)	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))	((*,*)((*,*)))

FIG. 10

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)				

*FIG. 11A*

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))

*FIG. 11B*

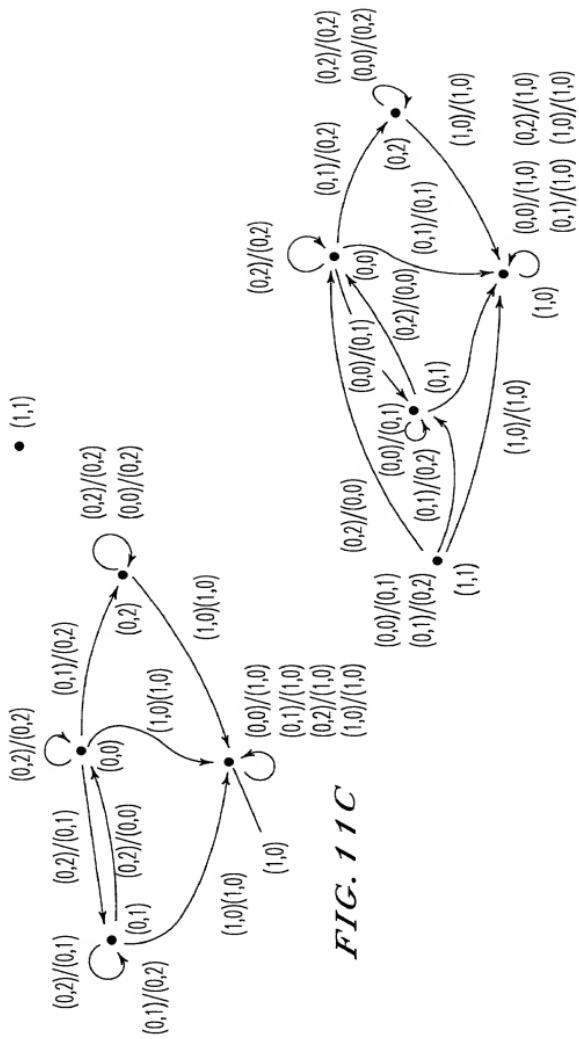


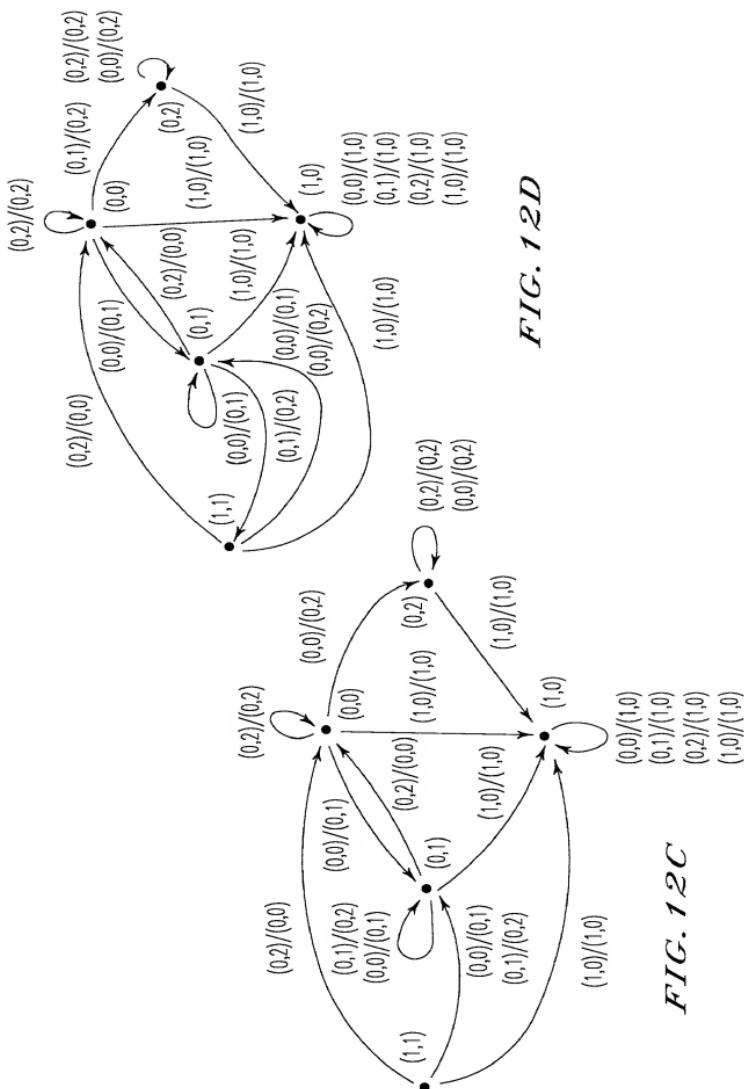
FIG. 11D

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))

*FIG. 12A*

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((1,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))

*FIG. 12B*



INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((0,1),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((1,0),(1,0))
(0,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((1,0),(1,0))
(1,0)	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))	((1,0),(1,0))
(1,1)	((0,1),(0,1))	((0,1),(0,2))	((0,0),(0,0))	((1,0),(1,0))

**FIG. 13A**

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((1,0),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((0,1),(1,0))
(0,1)	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((0,1),(1,0))
(1,0)	((1,0),(0,1))	((1,0),(0,2))	((0,0),(0,0))	((0,1),(1,0))
(1,1)	((1,0),(0,1))	((1,0),(0,2))	((0,0),(0,0))	((0,1),(1,0))

**FIG. 13B**

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
STATE				
(0,0)	((1,0),(0,1))	((0,2),(0,2))	((0,0),(0,2))	((0,1),(1,0))
(0,1)	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))
(0,2)	((0,2),(0,2))	—	((0,2),(0,2))	((0,1),(1,0))
(1,0)	((1,0),(0,1))	((1,0),(0,2))	((0,0),(0,0))	((0,1),(1,0))
(1,1)	((1,0),(0,1))	((1,0),(0,2))	((0,0),(0,0))	((0,1),(1,0))

**FIG. 14A**

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
STATE				
(0,0)	((1,0),(0,1))	((0,2),(0,2))	((0,1),(1,0))	((0,0),(0,2))
(0,1)	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))
(0,2)	((0,2),(0,2))	—	((0,1),(1,0))	((0,2),(0,2))
(1,0)	((1,0),(0,1))	((1,0),(0,2))	((0,1),(1,0))	((0,0),(0,0))
(1,1)	((1,0),(0,1))	((1,0),(0,2))	((0,1),(1,0))	((0,0),(0,0))

**FIG. 14B**

INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((1,0),(0,1))	((0,2),(0,2))	((0,1),(1,0))	((0,0),(0,2))
(0,1)	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))	((0,1),(1,0))
(0,2)	((0,2),(0,2))	—	((0,1),(1,0))	((0,2),(0,2))
(1,0)	((1,0),(0,1))	((1,0),(0,2))	((0,1),(1,0))	((0,0),(0,0))
(1,1)	((1,0),(0,1))	((1,0),(0,2))	((0,1),(1,0))	((0,0),(0,0))

**FIG. 15A**

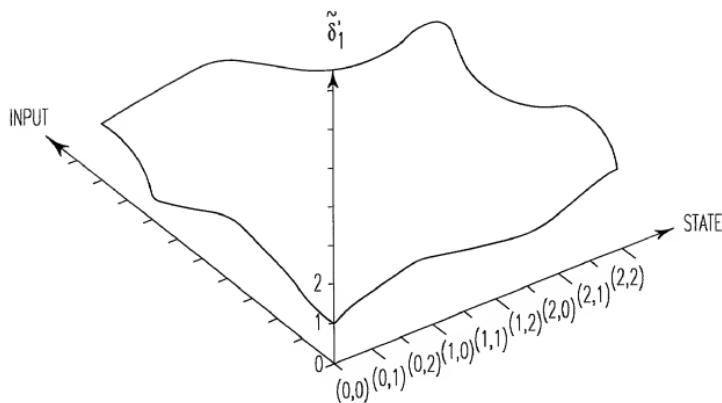
INPUT STATE \	(0,0)	(0,1)	(0,2)	(1,0)
(0,0)	((1,0),(0,1))	((0,2),(1,0))	((0,1),(0,2))	((0,0),(1,0))
(0,1)	((0,1),(0,2))	((0,1),(0,2))	((0,1),(0,2))	((0,1),(0,2))
(0,2)	((0,2),(1,0))	—	((0,1),(0,2))	((0,2),(1,0))
(1,0)	((1,0),(0,1))	((1,0),(1,0))	((0,1),(0,2))	((0,0),(0,0))
(1,1)	((1,0),(0,1))	((1,0),(1,0))	((0,1),(0,2))	((0,0),(0,0))

**FIG. 15B**

INPUT STATE	(0,0)	
(0,0)	((0,1)(0,1))	

*FIG. 16A*

09737742.121900



*FIG. 16B*

PRECALCULATE  $a_i(x)$  FOR  $k=\{0,1,2,4,5\} \subset Z_{11}$ .

PRECOMPUTATION RESULTS IN THE SERIES OF POLYNOMIALS

$$a_0(x)$$

$$a_1(x)$$

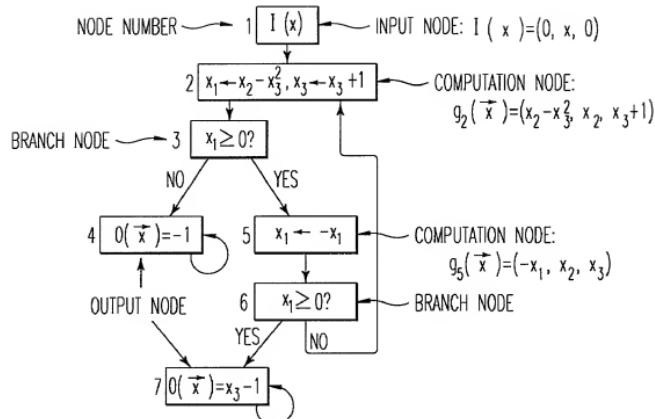
$$a_2(x)$$

$$a_4(x)$$

$$a_5(x)$$

REPRESENTED BY THEIR RESPECTIVE ARRAYS OF COEFFICIENTS

*FIG. 17*



- WHEN RESTRICTING A BSS MACHINE TO A FINITE FIELD  $\mathbb{Z}_N$ , THE CHOICE OF N IS DICTATED BY THE FOLLOWING:
  - 1) N MUST BE A PRIME NUMBER
  - 2) N MUST BE AT LEAST AS GREAT AS THE NUMBER OF NODES
  - 3) N MUST MAKE ALLOWANCE FOR CONSTANTS USED IN THE MACHINE
  - 4) N MUST ACCOMMODATE USER REQUIREMENTS
- FOR THE ABOVE EXAMPLE:
  - N SATISFIES THE FIRST CONDITION IF IT IS EQUAL TO 2, 3, 5, 7, 11, ...
  - N SATISFIES THE SECOND CONDITION IF IT IS  $\geq 7$
  - N THE GREATEST CONSTANTS HAVE ABSOLUTE VALUE 1, SO N SATISFIES THE THIRD CONDITION IF IT IS  $\geq 2$
  - IF THE USER REQUIRES THAT THE x INPUT MUST BE ABLE TO BE AS LARGE AS 100, N SATISFIES THE FOURTH CONDITION IF IT IS  $> 100$ . THE LEAST N SATISFYING ALL FOUR CONDITIONS WOULD THEN BE N=101
- SINCE ALL MAPPINGS IN THE BSS MACHINE ABOVE ARE POLYNOMIAL, THE RESTRICTION OF COMPUTATION MAPPINGS TO POLYNOMIAL MAPPINGS IS ALREADY SATISFIED.
- THE NEW NODE-NUMBERING CONVENTION SIMPLY SUBTRACTS 1 FROM EACH NODE NUMBER, SUCH THAT NUMBERING BEGINS AT 0. 1 2 3 4 5 6 7
 
$$\begin{matrix} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{matrix}$$

**FIG. 18**

THE FULL STATE SPACE OF THE BSS MACHINE, AS ADAPTED SO FAR, IS:

$$\underbrace{\{0, \dots, 6\}}_{\text{NODE NUMBER SPACE}} \times \underbrace{Z_N^x \times Z_N^x \times Z_N^x}_{\text{STATE SPACE}} \quad \text{CORRESPONDING VECTORS HAVE THE COMPONENTS:}$$

$\pi$	$x_1$	$x_2$	$x_3$
-------	-------	-------	-------

THE REVISED FULL STATE SPACE ADDS THE OUTPUT AND INPUT COMPONENTS:

$$\underbrace{\{0, \dots, 6\}}_{\text{NODE NUMBER SPACE}} \times \underbrace{Z_N^x \times Z_N^x \times Z_N^x \times Z_N^x \times Z_N^x}_{\text{OUTPUT INPUT}} \quad \text{CORRESPONDING VECTORS HAVE THE COMPONENTS:}$$

$\pi$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$
-------	-------	-------	-------	-------	-------

INPUT  
OUTPUT

ALSO A COMPUTATION MAPPING  $g_i$  IS ADDED TO EVERY NODE THAT DOESN'T ALREADY HAVE ONE. THUS FOR EACH NODE VIEWED IN ISOLATION:

- NODE 0:  $g_0(\vec{x}) = (0, x_5, 0, 0, x_5)$  IS ADDED
- NODE 1: " $g_2$ " (NOW  $g_1$ ) IS CHANGED TO  $g_1(\vec{x}) = (x_2 - x_3^2, x_2, x_3 + 1, 0, x_5)$
- NODE 2:  $g_2(\vec{x}) = (x_1, x_2, x_3, 0, x_5)$  IS ADDED
- NODE 3:  $g_3(\vec{x}) = (x_1, x_2, x_3^{N-1}, x_5)$  IS ADDED
- NODE 4:  $g_4$  (PREVIOUSLY " $g_5$ ") IS CHANGED TO  $g_4(\vec{x}) = (-x_1, x_2, x_3, 0, x_5)$
- NODE 5:  $g_5(\vec{x}) = (x_1, x_2, x_3, 0, x_5)$  IS ADDED
- NODE 6:  $g_6(\vec{x}) = (x_1, x_2, x_3, x_3 - 1, x_5)$  IS ADDED

AS THE RELATION  $\geq 0$  HOLDS FOR ALL ELEMENTS IN  $Z_N^x$ , IT IS REPLACED BY A SERIES OF SET INCLUSION RELATIONS. BECAUSE  $Z_N$  DOES NOT HAVE NEGATIVE NUMBERS AS ELEMENTS, THE RELATIONS WILL NOT HAVE AN EXACT CORRESPONDENCE TO THE ORIGINAL RELATIONS. REASONABLE SET INCLUSION RELATIONS FOR THIS EXAMPLE ARE:

FOR NODE 2:  $\in Z_p - \{0\}$  WITH THE SAME MAPPING IN NODE 1 AS BEFORE.  
FOR NODE 5:  $\in \{1\}$ , CHANGING  $g_4$  TO  $g_4(\vec{x}) = (x_3 + 1, x_2, x_3, 0, x_5)$

FIG. 19

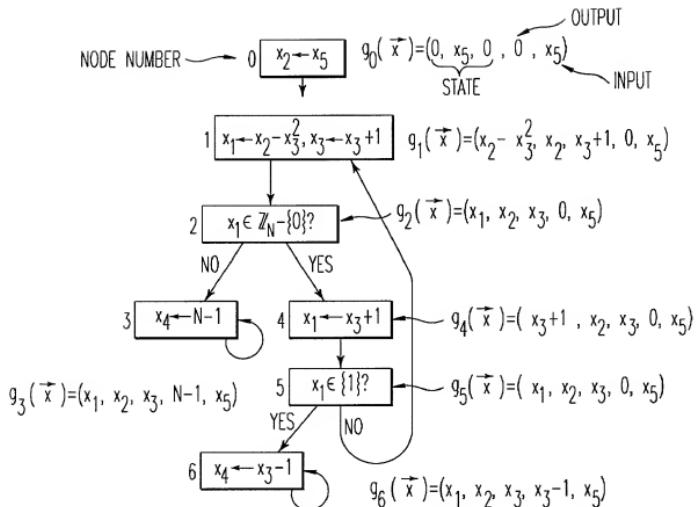


FIG. 20A

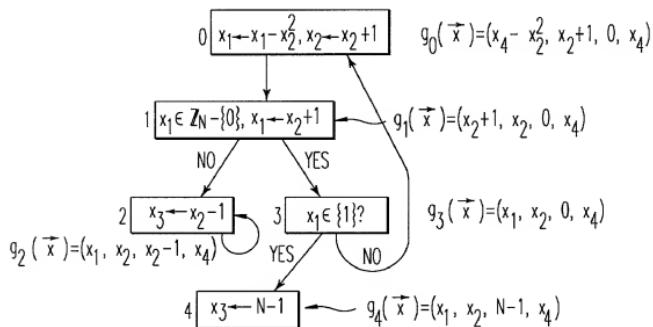
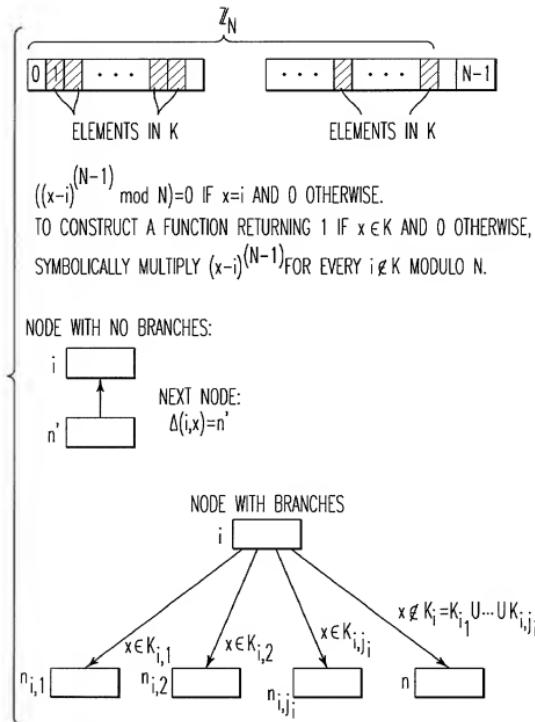


FIG. 20B

**FIG. 21**

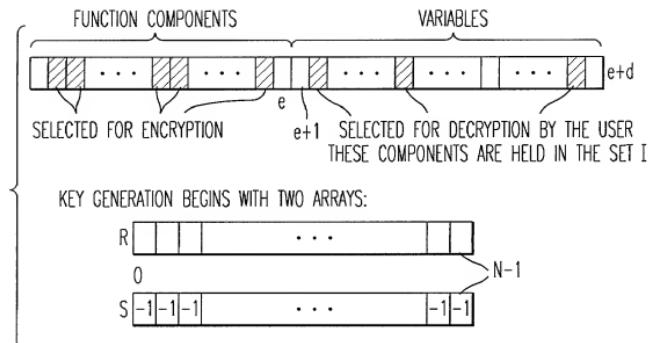


FIG. 22A

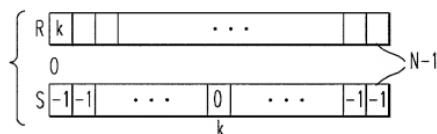


FIG. 22B

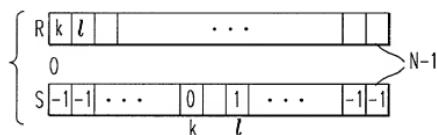
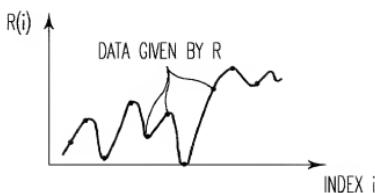


FIG. 22C



*FIG. 23*

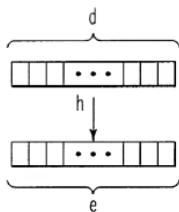
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X\Y	0	1	2	3	4
0	0	0	0	0	0
1	0	1	2	3	4
2	0	2	4	1	3
3	0	3	1	4	2
4	0	4	3	2	1

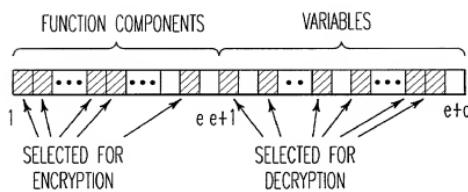
*FIG. 24A*

X\Y	0	1	2	3	4
0	1	0	0	0	0
1	1	1	1	1	1
2	1	2	4	3	1
3	1	3	4	2	1
4	1	4	1	4	1

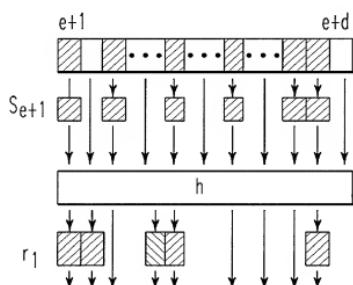
*FIG. 24B*



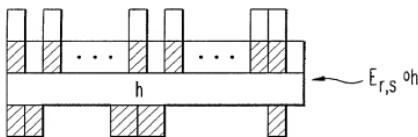
**FIG. 25A**



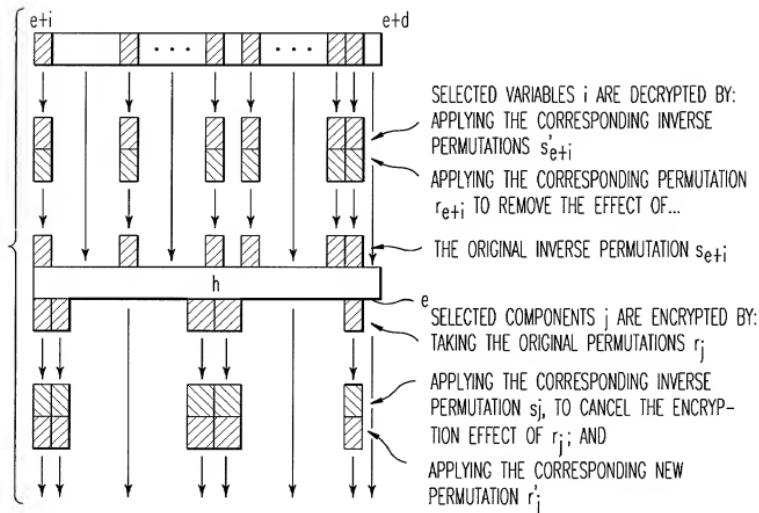
**FIG. 25B**



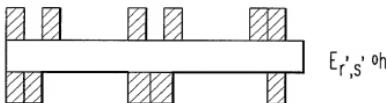
**FIG. 25C**



*FIG. 26A*



*FIG. 26B*



*FIG. 26C*

$x_1$	$x_2$	0	1	2	3	4
0	(3,4)	(1,2)	(4,0)	(2,1)	(1,3)	
1	(0,0)	(2,3)	(3,4)	(4,1)	(0,2)	
2	(2,0)	(3,2)	(1,2)	(0,1)	(1,4)	
3	(4,0)	(2,0)	(4,4)	(4,4)	(2,4)	
4	(1,1)	(2,2)	(1,0)	(4,1)	(4,2)	

FIG. 27A

X	0	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
f	1	23	2	4	6	11	17	13	2	12	4	23	11	24	1	7	9	5	24	9	16	10	21	14

FIG. 27B

FUNCTION TABLE FOR f

1	2	3	4	5
---	---	---	---	---

FUNCTION TABLE FOR f

1	2	3	4	5
---	---	---	---	---

FIG. 27C

FIG. 27D

$X_1 \backslash X_2$	0	1	2	3	4
0	0	1	3	2	0
1	2	2	4	2	0
2	1	0	4	2	1
3	2	3	3	2	1
4	2	0	1	1	2

**FIG. 28A**

X	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
t <sub>f</sub>	23	0	2	4	6	11	17	13	2	12	4	23	11	24	1	7	9	5	24	9	16	10	21	22	14

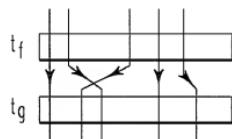
**FIG. 28B**

X	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	13	16	17	18	19	20	21	22	23	24
t <sub>g</sub>	0	2	1	2	2	1	2	0	3	0	3	4	4	3	1	2	2	2	2	1	0	0	1	1	2

**FIG. 28C**

X	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
t <sub>f</sub>	1	0	1	2	2	4	2	3	1	4	2	1	4	2	2	0	0	1	2	0	2	3	0	1	1

**FIG. 28D**



**FIG. 28E**

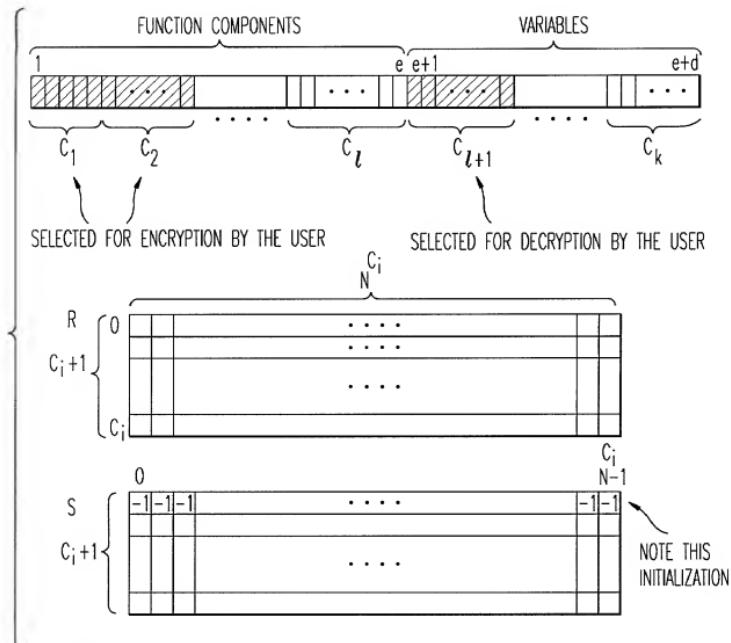


FIG. 29A

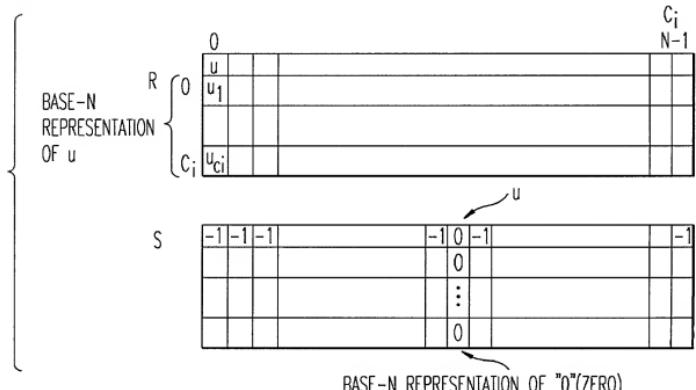
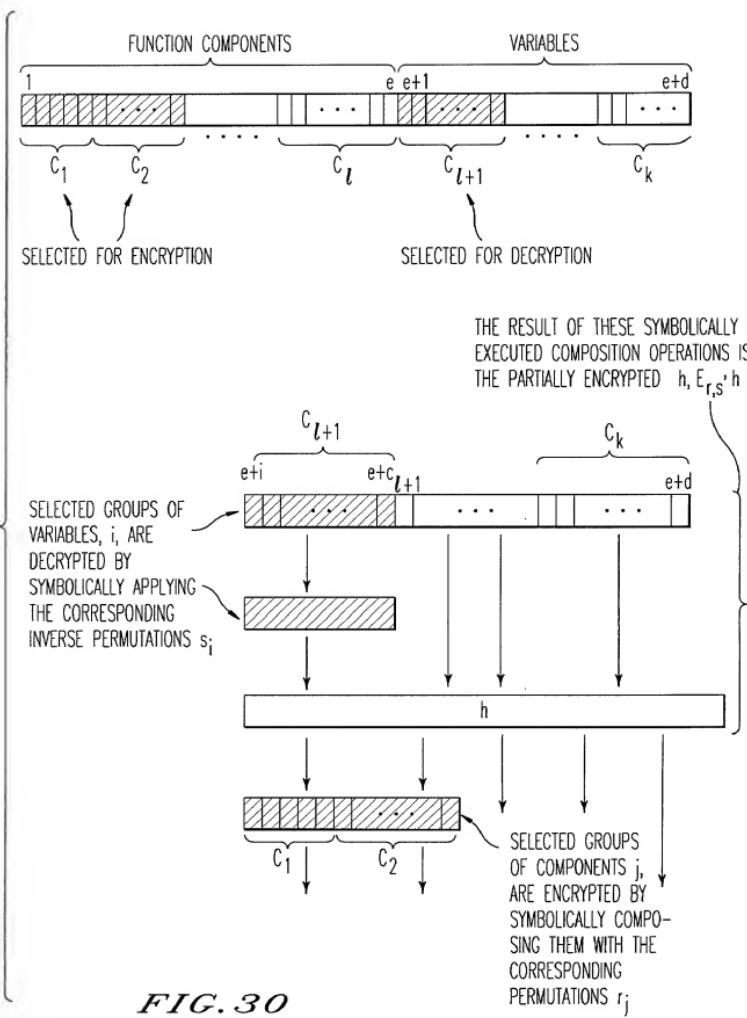
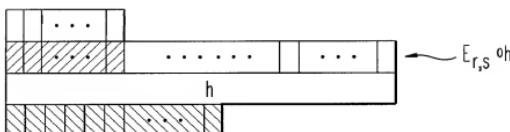


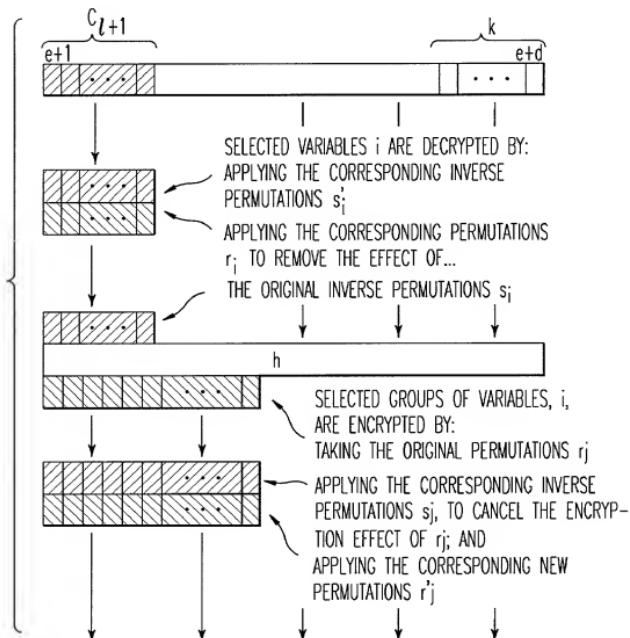
FIG. 29B



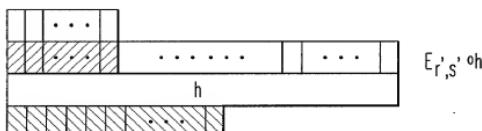
**FIG. 30**



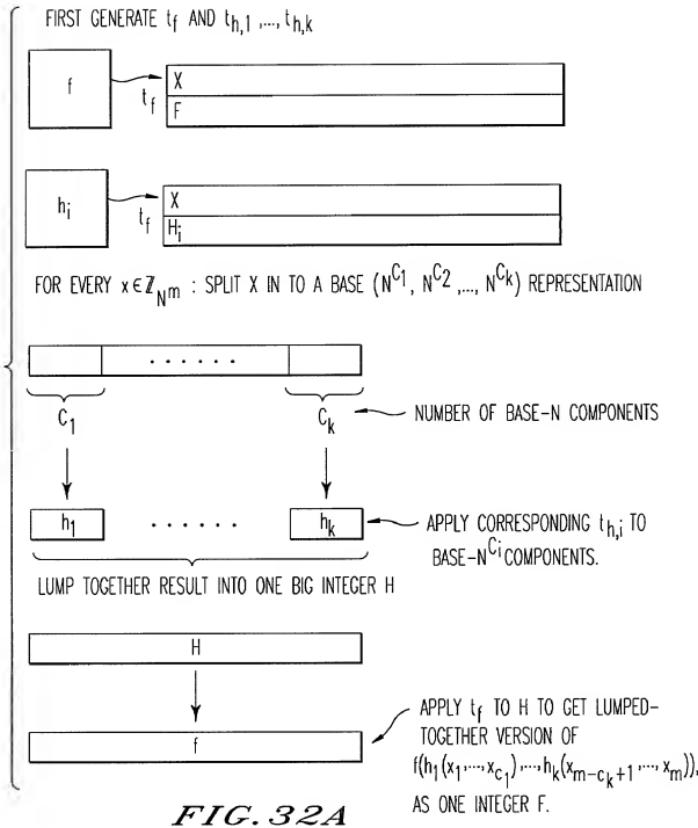
*FIG. 31A* C



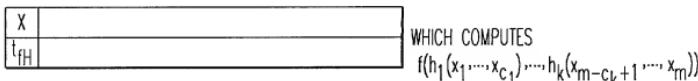
*FIG. 31B*



*FIG. 31C*

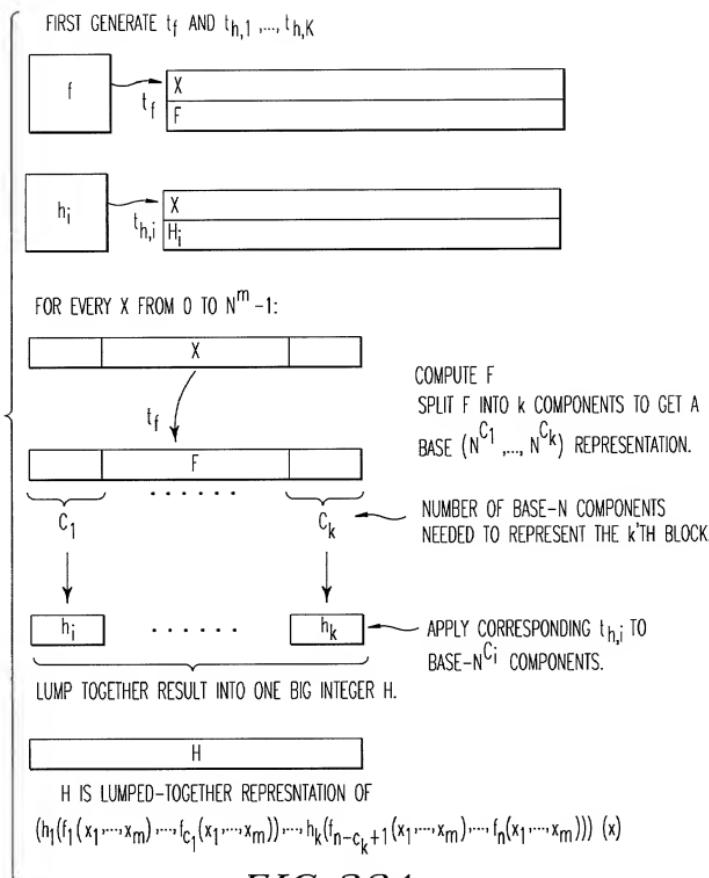


**FIG. 32A**



**FIG. 32B**

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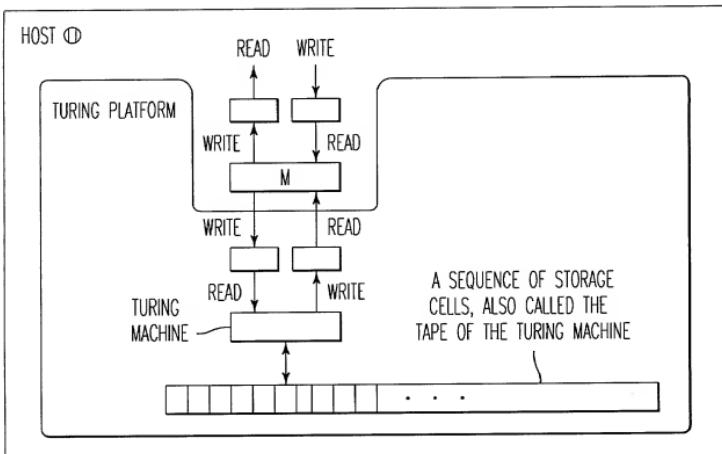
**FIG. 33A**



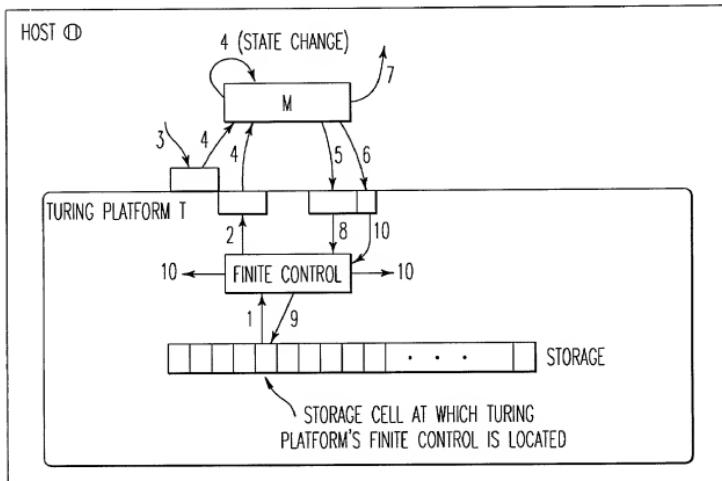
THAT COMPUTES  $(x)$ ,

**FIG. 33B**

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*FIG. 34*



*FIG. 35*

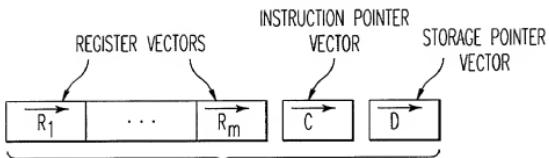


FIG. 36A

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SHARED DATA IN THE  
FORM OF D-VECTORS

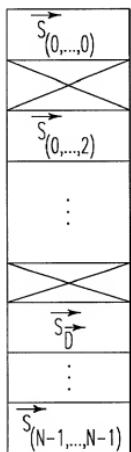


FIG. 36B

SET OF INSTRUCTIONS  
 $P$

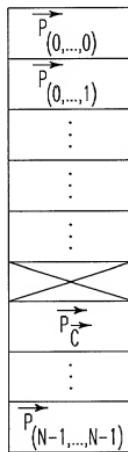


FIG. 36C

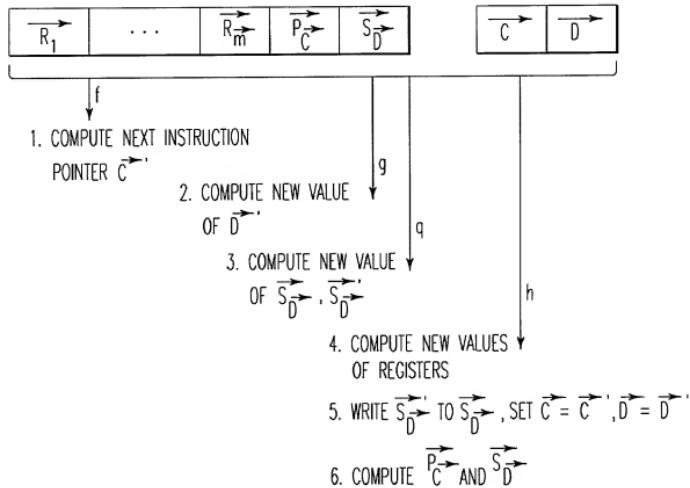


FIG. 36D

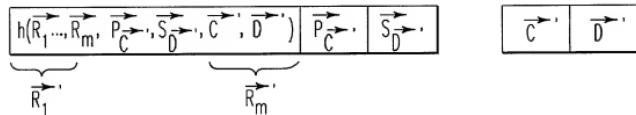


FIG. 36E

$h_1: \mathbb{Z}_2^2 \rightarrow \mathbb{Z}_2^2$	
$\vec{x}$	$h(\vec{x})$
(0,0)	(1,0)
(0,1)	(1,1)
(1,0)	(0,0)
(1,1)	(0,1)

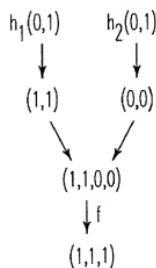
$h_2: \mathbb{Z}_2^2 \rightarrow \mathbb{Z}_2^2$	
$\vec{x}$	$h(\vec{x})$
(0,0)	(1,1)
(0,1)	(0,0)
(1,0)	(1,0)
(1,1)	(1,0)

**FIG. 37A**

$f: \mathbb{Z}_2^4 \rightarrow \mathbb{Z}_2^3$	
$\vec{x}$	$f(\vec{x})$
(0,0,0,0)	(1,0,1)
(0,0,0,1)	(0,0,1)
(0,0,1,0)	(1,0,1)
(0,0,1,1)	(0,0,0)
(0,1,0,0)	(1,0,0)
(0,1,0,1)	(0,0,0)
(0,1,1,0)	(1,1,1)
(0,1,1,1)	(1,0,0)
(1,0,0,0)	(1,1,0)
(1,0,0,1)	(0,0,1)
(1,0,1,0)	(0,1,1)
(1,0,1,1)	(1,0,1)
(1,1,0,0)	(1,1,1)
(1,1,0,1)	(0,0,0)
(1,1,1,0)	(1,1,0)
(1,1,1,1)	(0,1,0)

**FIG. 37B**

$g: \mathbb{Z}_2^3 \rightarrow \mathbb{Z}_2^3$	
$\vec{x}$	$g(\vec{x})$
(0,0,0)	(1,0,1)
(0,0,1)	(0,0,0)
(0,1,0)	(1,1,1)
(0,1,1)	(1,0,0)
(1,0,0)	(0,1,1)
(1,0,1)	(1,0,1)
(1,1,0)	(1,1,0)
(1,1,1)	(1,1,1)

**FIG. 37C****FIG. 37D**

$$f: \mathbb{Z}_2^4 \rightarrow \mathbb{Z}_2^3$$

$\vec{x}$	$f(\vec{x})$
(0,0,0,0)	(1,0,1)
(0,0,0,1)	(0,0,1)
(0,0,1,0)	(1,0,1)
(0,0,1,1)	(0,0,0)
(0,1,0,0)	(1,0,0)
(0,1,0,1)	(0,0,0)
(0,1,1,0)	(1,1,1)
(0,1,1,1)	(1,0,0)
(1,0,0,0)	(1,1,0)
(1,0,0,1)	(0,0,1)
(1,0,1,0)	(0,1,1)
(1,0,1,1)	(1,0,1)
(1,1,0,0)	(1,1,1)
(1,1,0,1)	(0,0,0)
(1,1,1,0)	(1,1,0)
(1,1,1,1)	(0,1,0)

FIG. 38A

$$h_1: \mathbb{Z}_2^2 \rightarrow \mathbb{Z}_2^2$$

$\vec{x}$	$h_1(\vec{x})$
(0,0)	(1,0)
(0,1)	(1,1)
(1,0)	(0,0)
(1,1)	(0,1)

$$h_2: \mathbb{Z}_2^2 \rightarrow \mathbb{Z}_2^2$$

$\vec{x}$	$h_2(\vec{x})$
(0,0)	(1,1)
(0,1)	(0,0)
(1,0)	(1,0)
(1,1)	(1,0)

FIG. 38B

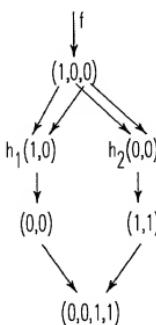


FIG. 38D

$$g: \mathbb{Z}_2^4 \rightarrow \mathbb{Z}_2^4$$

$\vec{x}$	$g(\vec{x})$
(0,0,0,0)	(0,0,0,0)
(0,0,0,1)	(1,1,0,0)
(0,0,1,0)	(0,1,0,0)
(0,0,1,1)	(1,0,1,1)
(0,1,0,0)	(0,0,1,0)
(0,1,0,1)	(1,0,1,1)
(0,1,1,0)	(0,1,1,0)
(0,1,1,1)	(0,0,1,1)
(1,0,0,0)	(0,0,1,0)
(1,0,0,1)	(1,1,0,0)
(1,0,1,0)	(1,1,1,0)
(1,0,1,1)	(0,1,0,0)
(1,1,0,0)	(0,1,1,0)
(1,1,0,1)	(1,0,1,1)
(1,1,1,0)	(0,0,1,0)
(1,1,1,1)	(1,0,1,0)

FIG. 38C

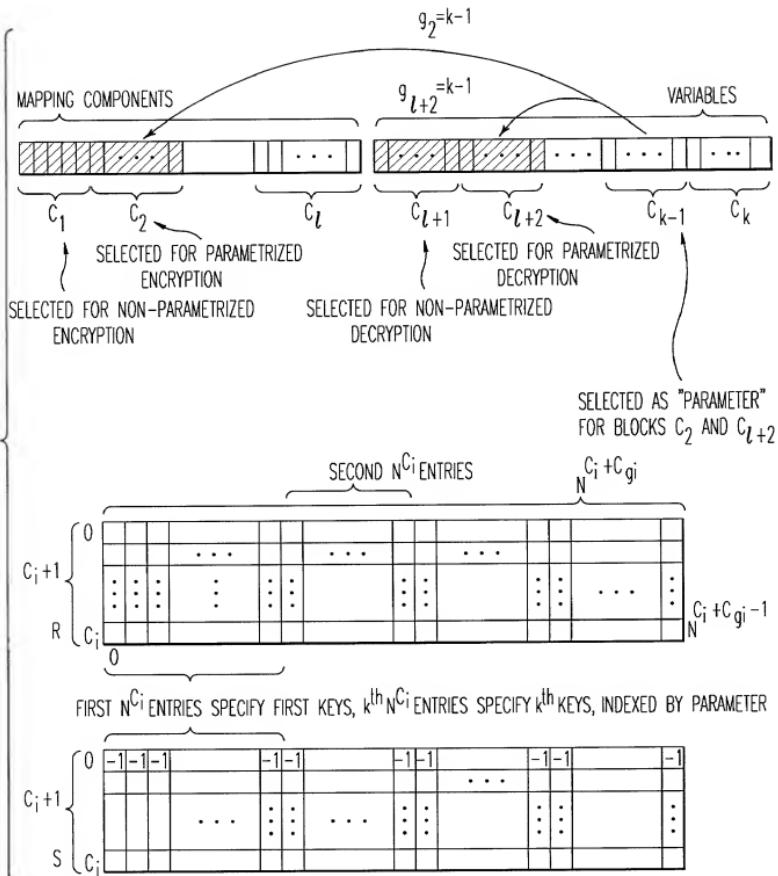


FIG. 39A

卷之三

R	46	7	3		9	u						
	⋮	⋮	⋮		⋮	⋮						⋮
					⋮	⋮						⋮
						⋮						⋮
						⋮						⋮
S	16	17	36	⋮	⋮	14 - 1	- 1   0   - 1					- 1
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮				⋮
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮				⋮
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮				⋮
	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮				⋮

FIG. 39B

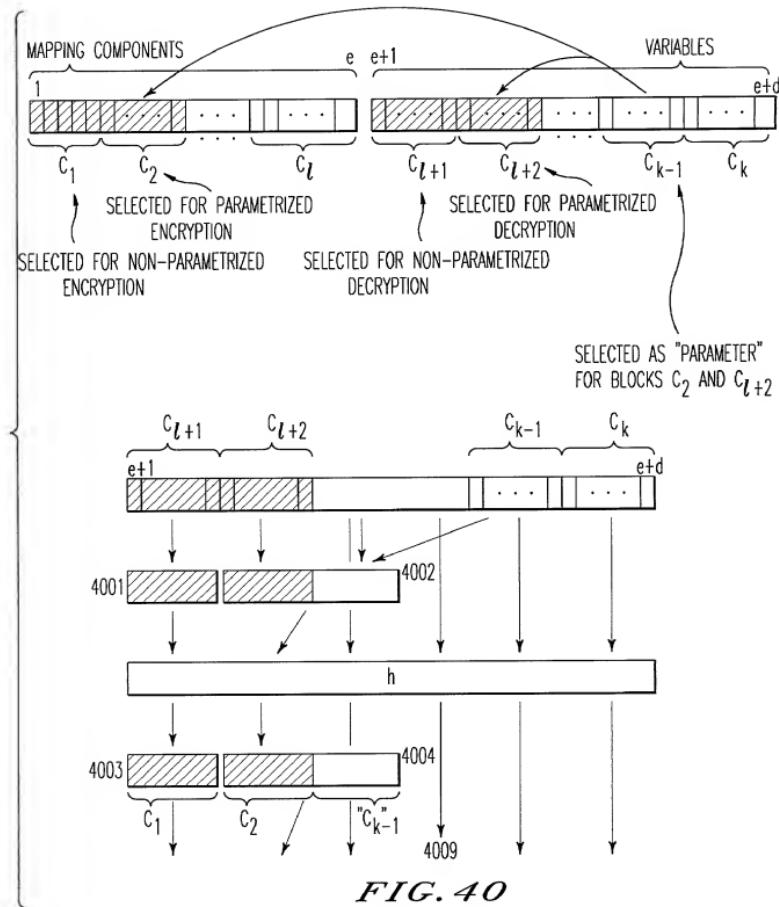
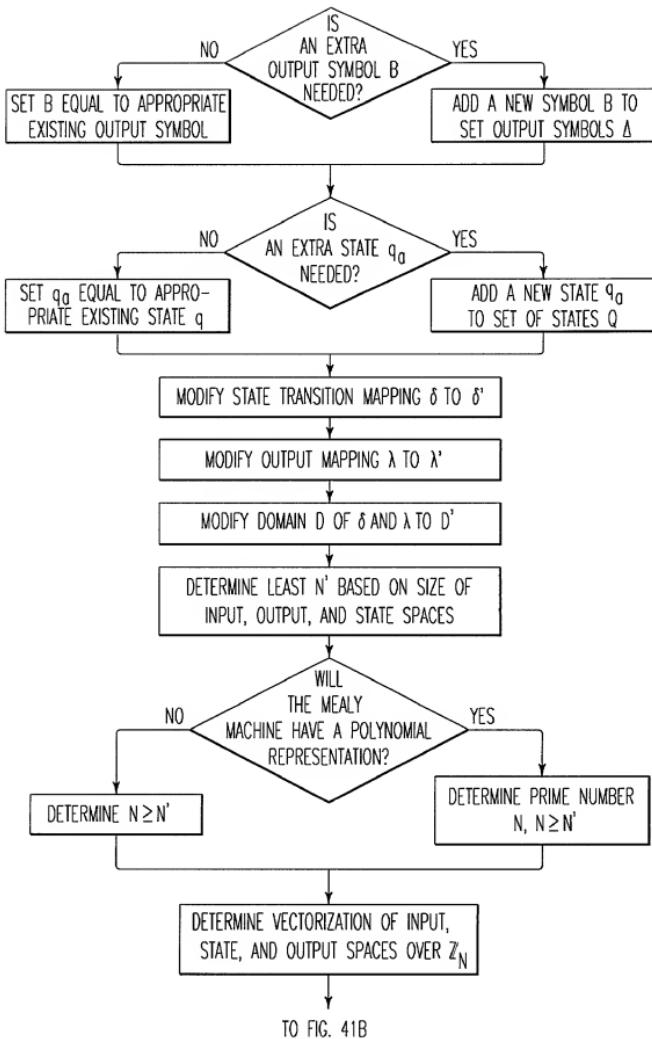


FIG. 40



**FIG. 41A**

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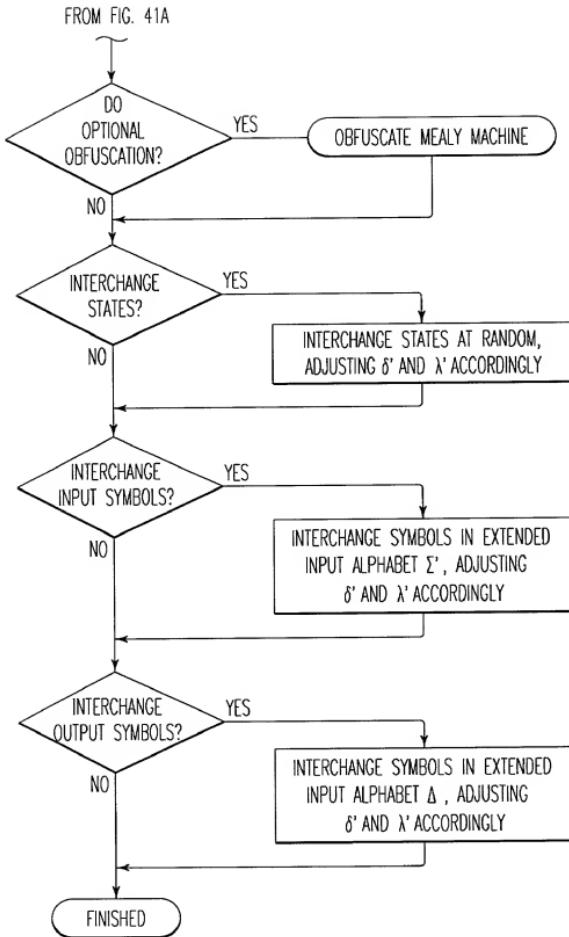


FIG. 41B

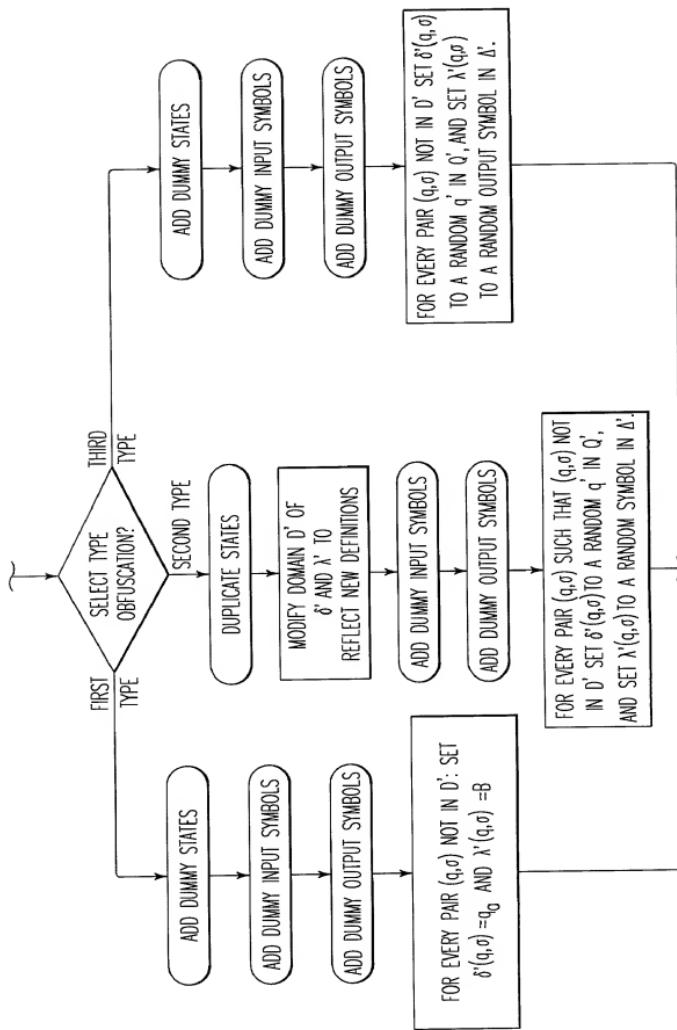
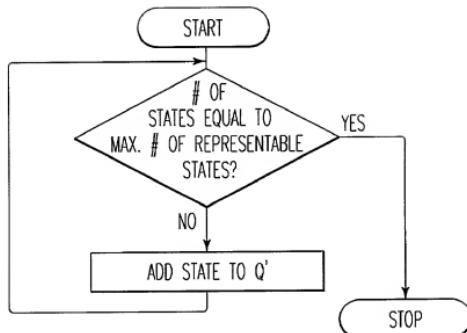
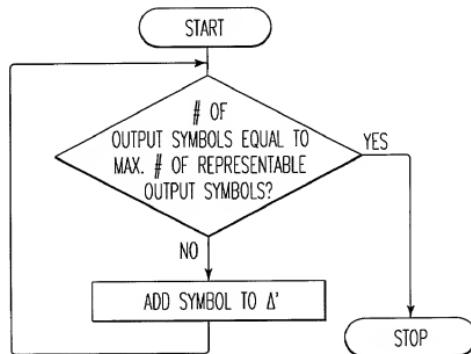
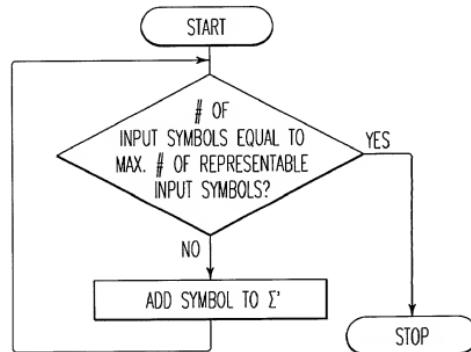


FIG. 4.2A

*FIG. 42B**FIG. 42C**FIG. 42D*

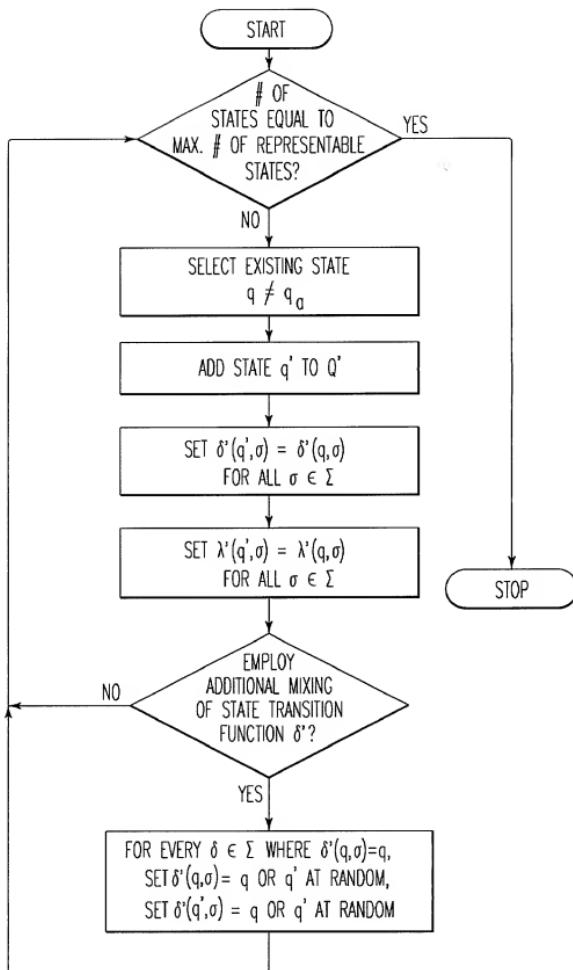


FIG. 42E

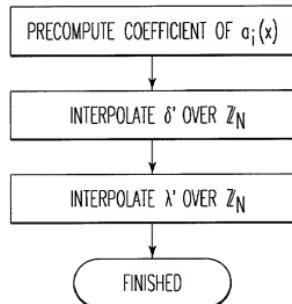


FIG. 43A

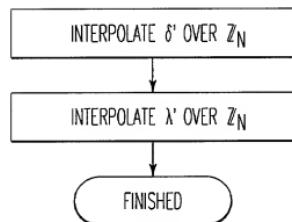
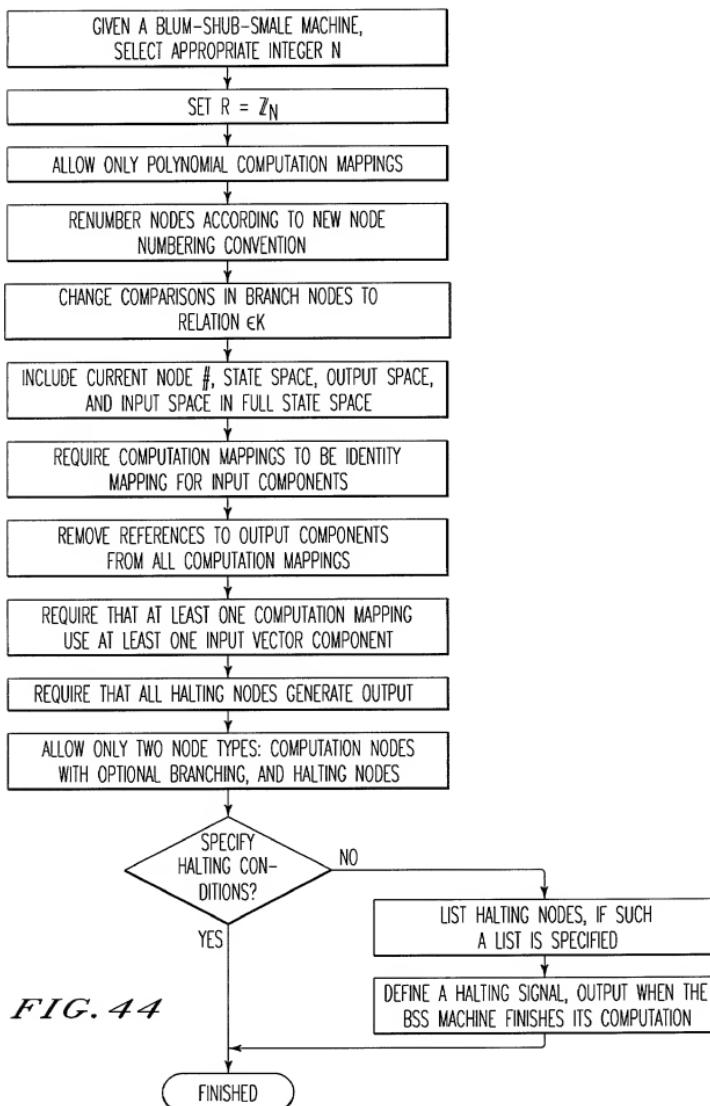


FIG. 43B



*FIG. 44*

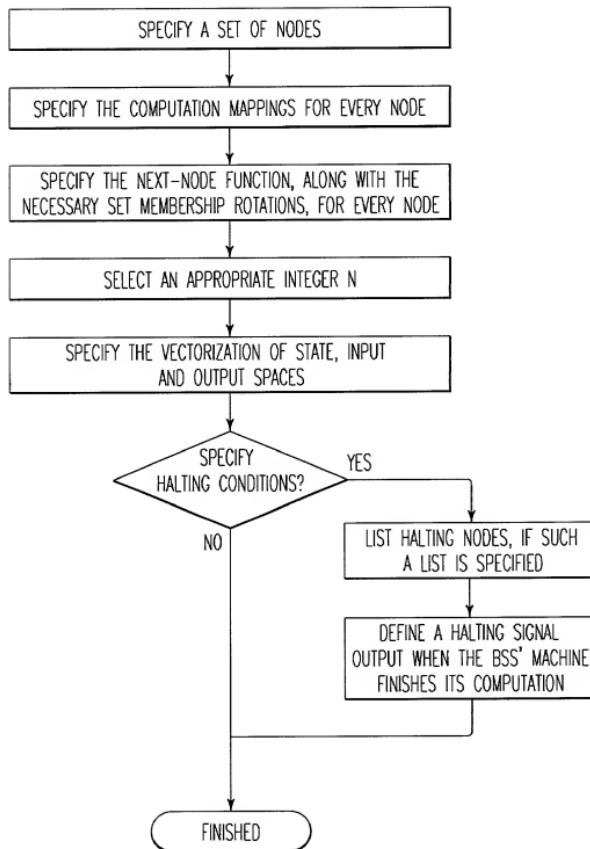
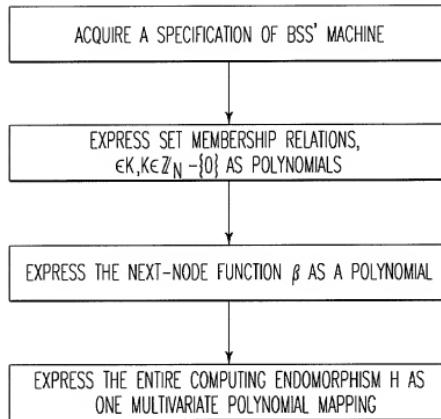


FIG. 45



*FIG. 46*

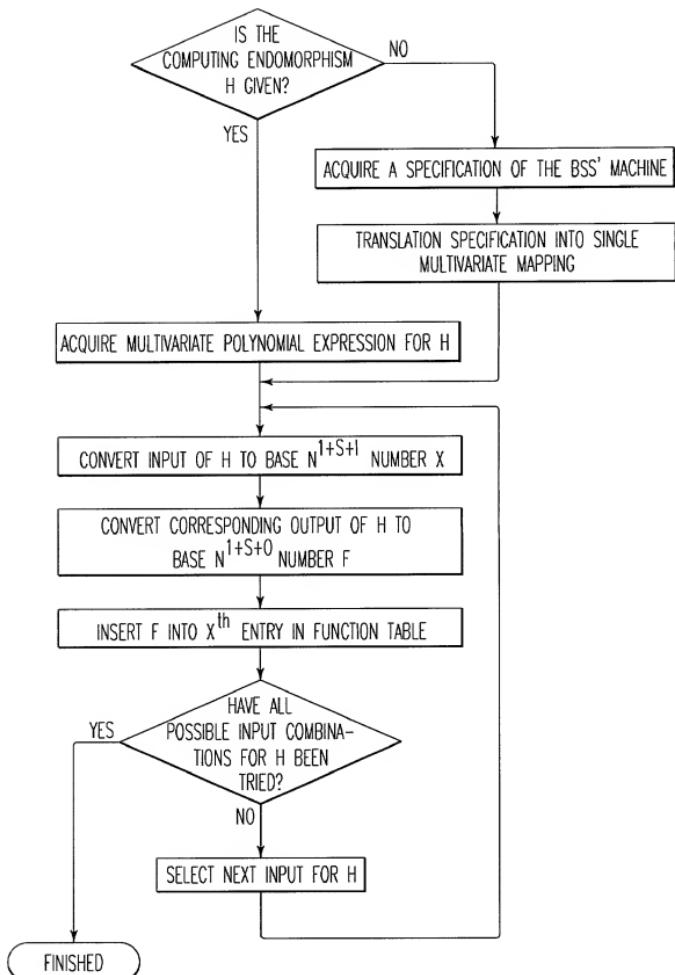
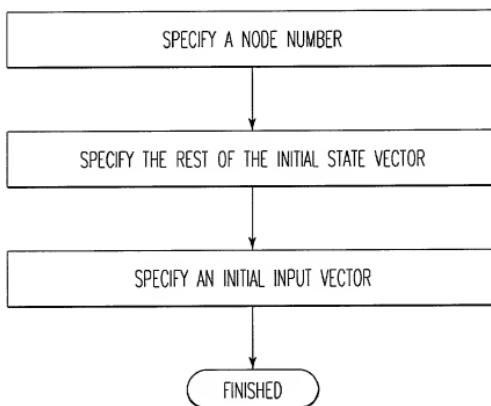


FIG. 47

09737742 • 121800



*FIG. 48*

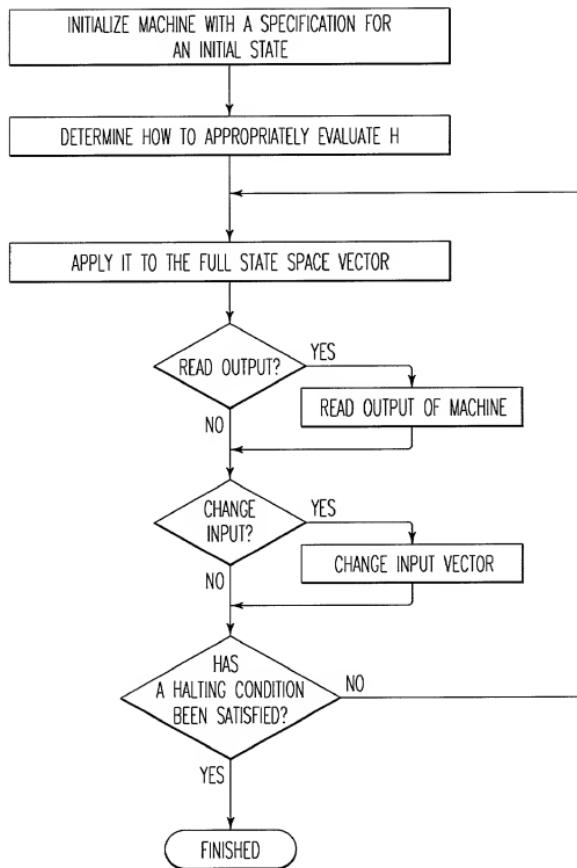
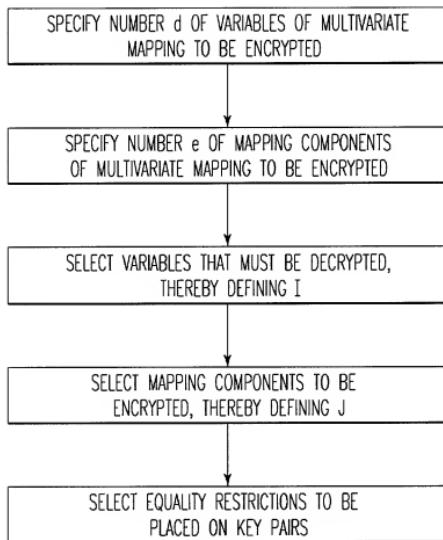


FIG. 49



*FIG. 50*

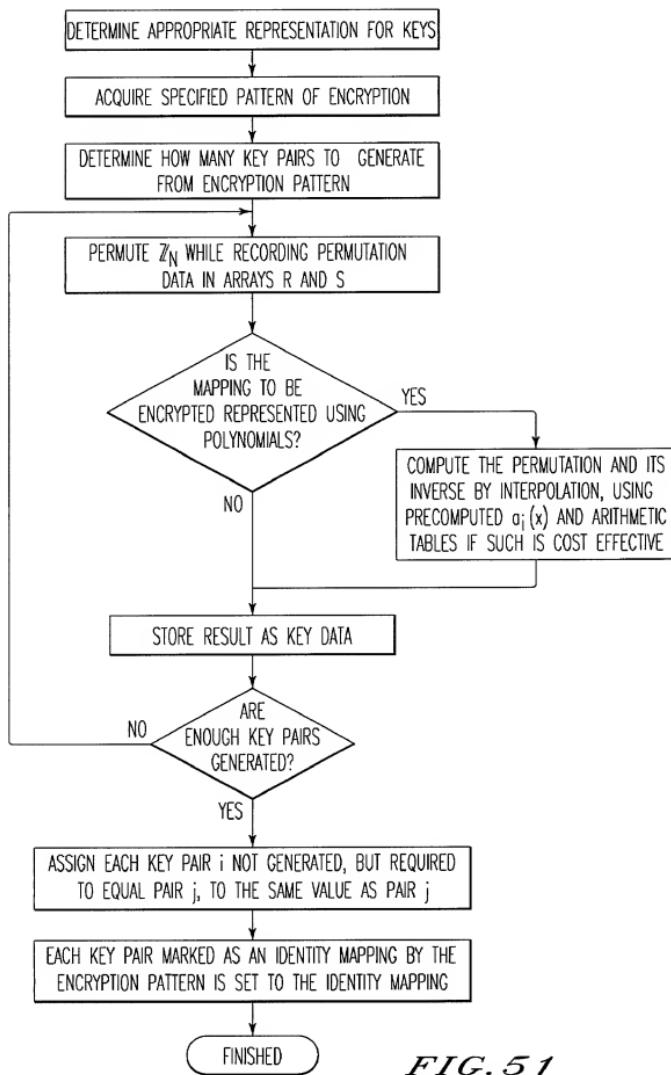
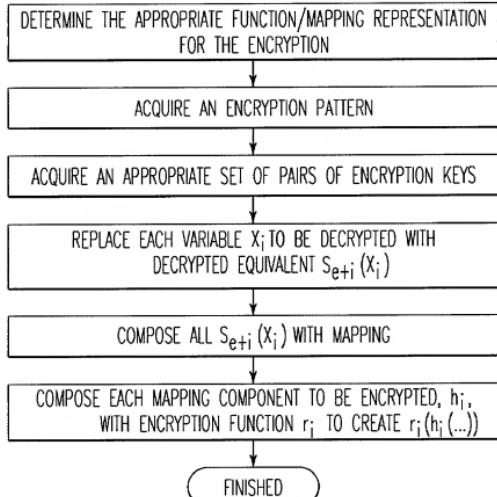
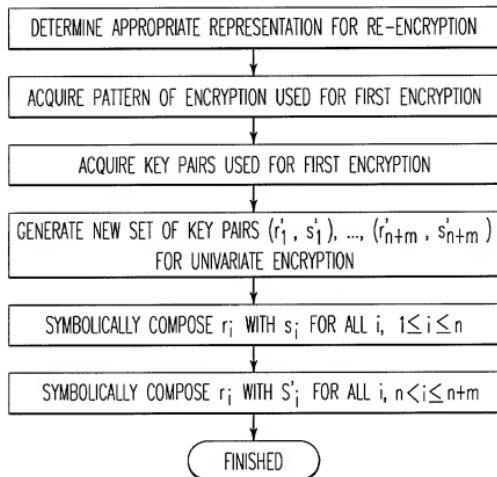


FIG. 51



**FIG. 52**



**FIG. 53**

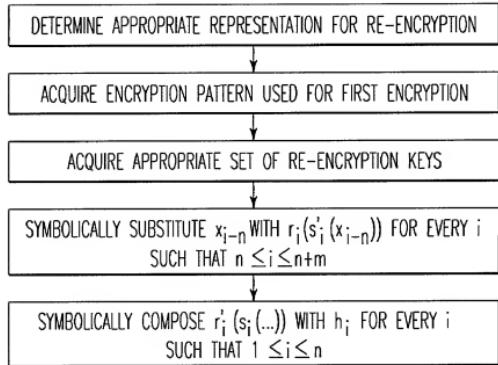


FIG. 54

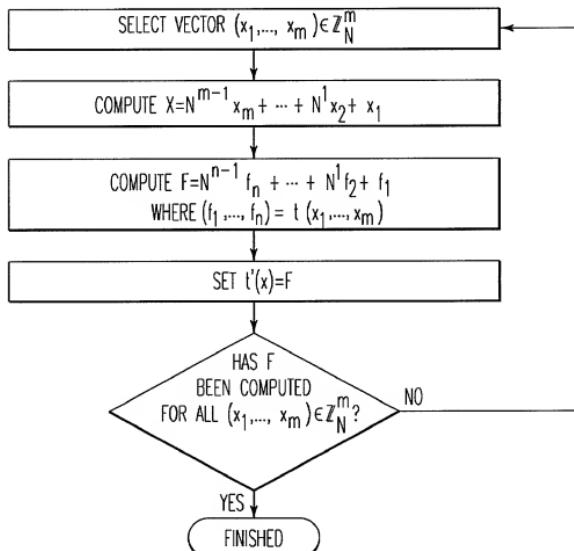


FIG. 55

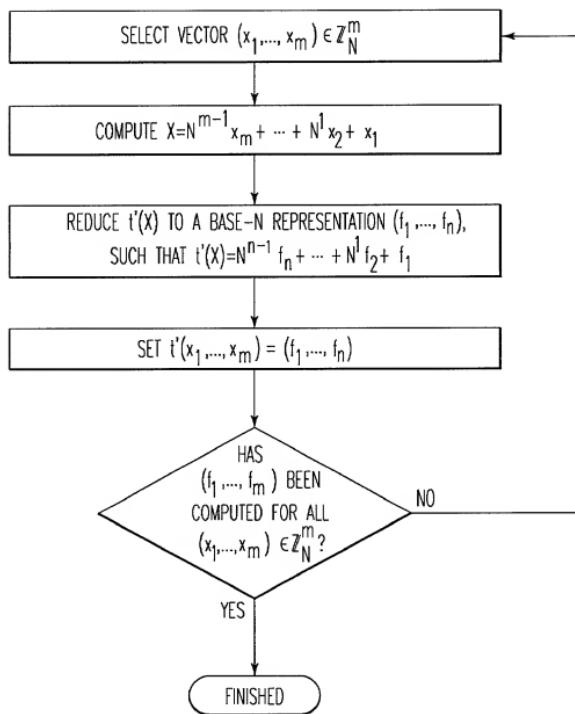


FIG. 56

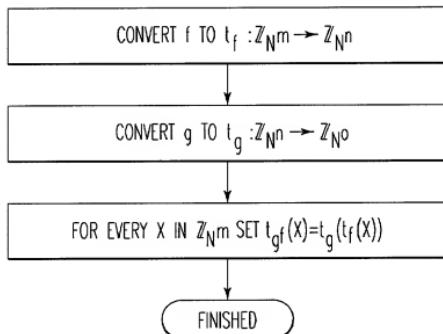


FIG. 57

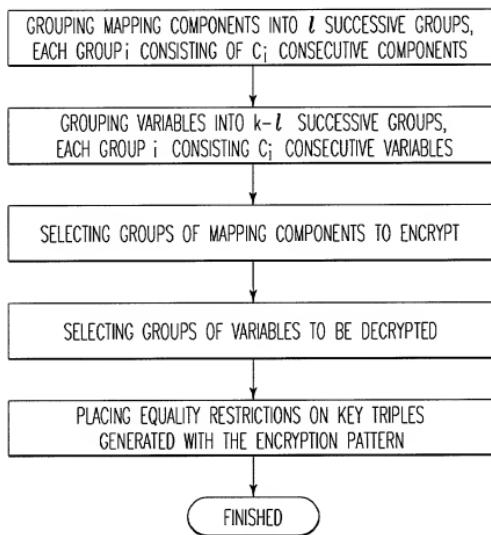


FIG. 58

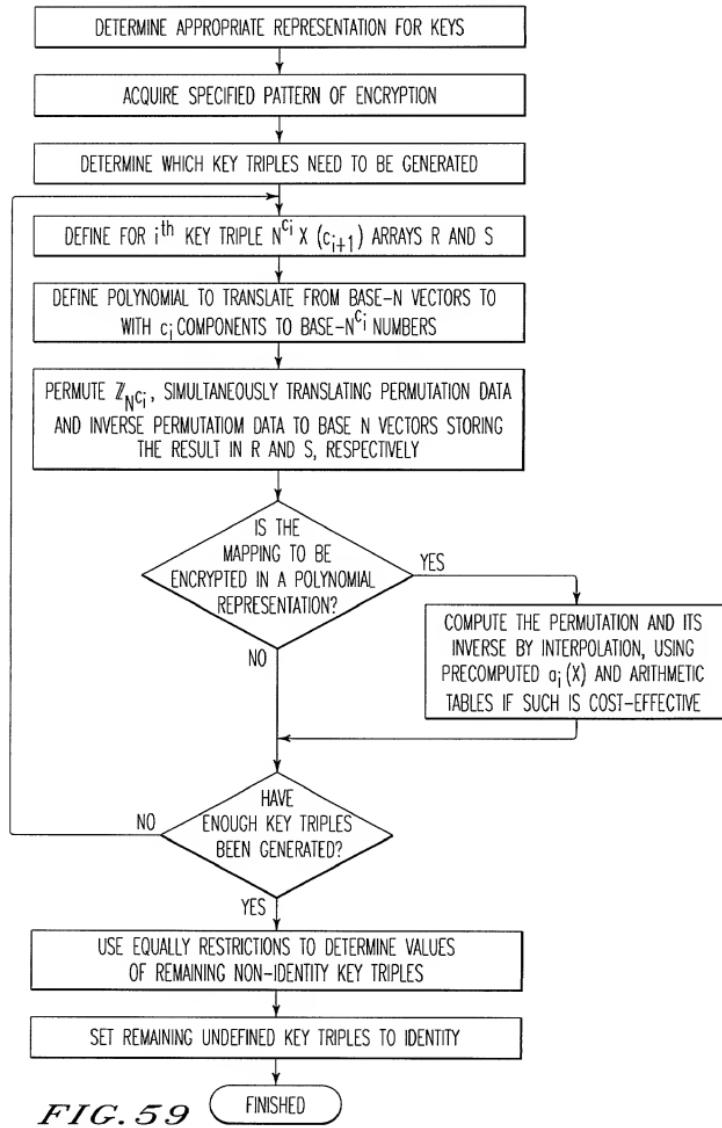


FIG. 59

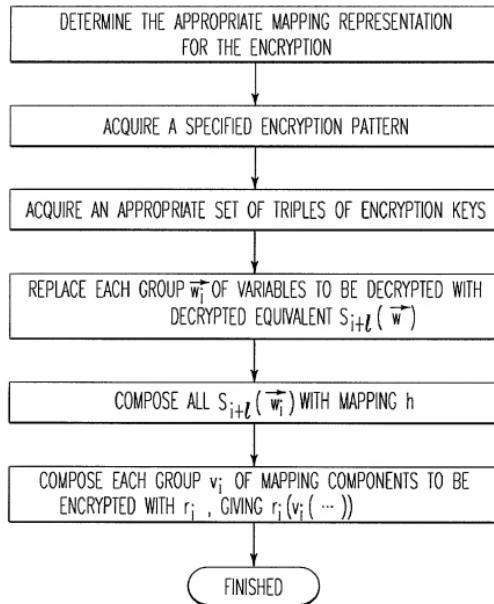
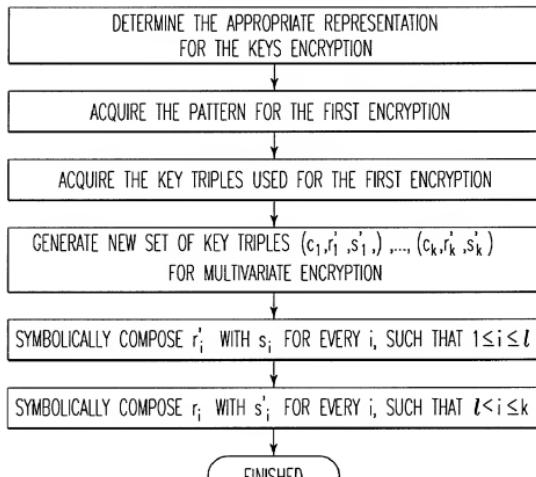
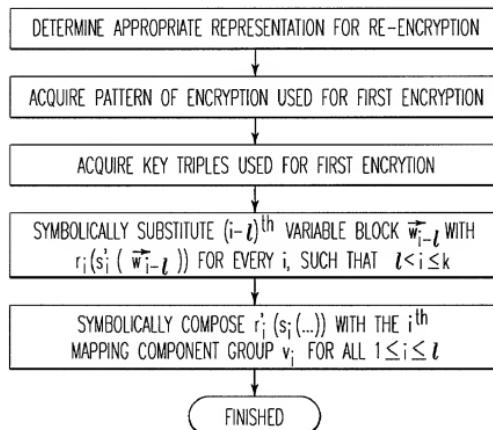


FIG. 60

**FIG. 61****FIG. 62**

ACQUIRE SPECIFICATION FOR THE  $c_i$  SUCH N THAT  $\sum_{i=1}^k c_i = m$

CONVERT  $f$  TO  $t_f : \mathbb{Z}_{N^m} \rightarrow \mathbb{Z}_{N^n}$

CONVERT EVERY  $h_i$  TO  $t_{h,i} : \mathbb{Z}_{N^{c_i}} \rightarrow \mathbb{Z}_{N^{c_i}}$

COMPUTE  $y_i = N^{c_i}$  FOR EVERY  $i$  FROM 1 TO  $k$

SET  $i=0$  AND  $(b_1, \dots, b_k) = (0, \dots, 0)$

SET  $u=0$  AND  $j=k$

SET  $u=y_j u + t_{h,j}(b_j)$

$j=j-1$

$j \leq 0?$

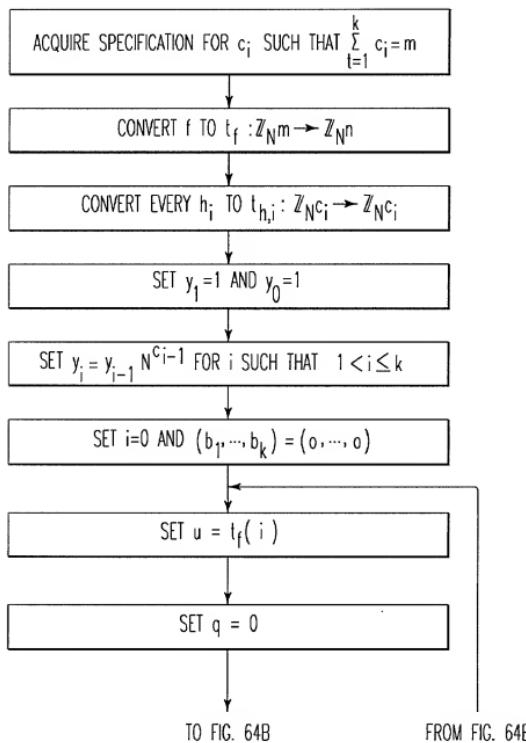
SET  $t_{fh}(i) = t_f(u)$

$i=i+1$  AND INCREMENT  $(b_1, \dots, b_k)$  AS A BASE  $(y_1, \dots, y_k)$  NUMBER

$i \geq N^m?$

FINISHED

**FIG. 63**



**FIG. 64A**

TO FIG. 64A

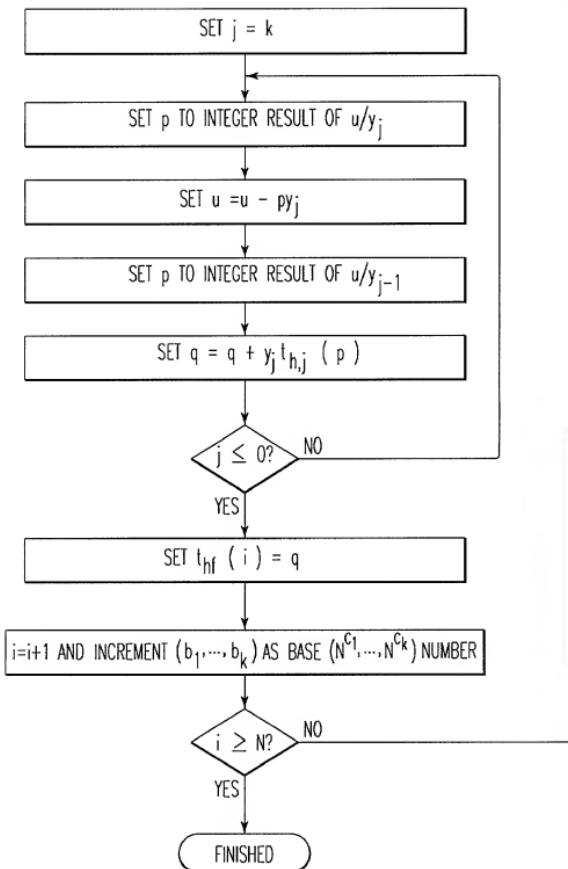


FIG. 64B

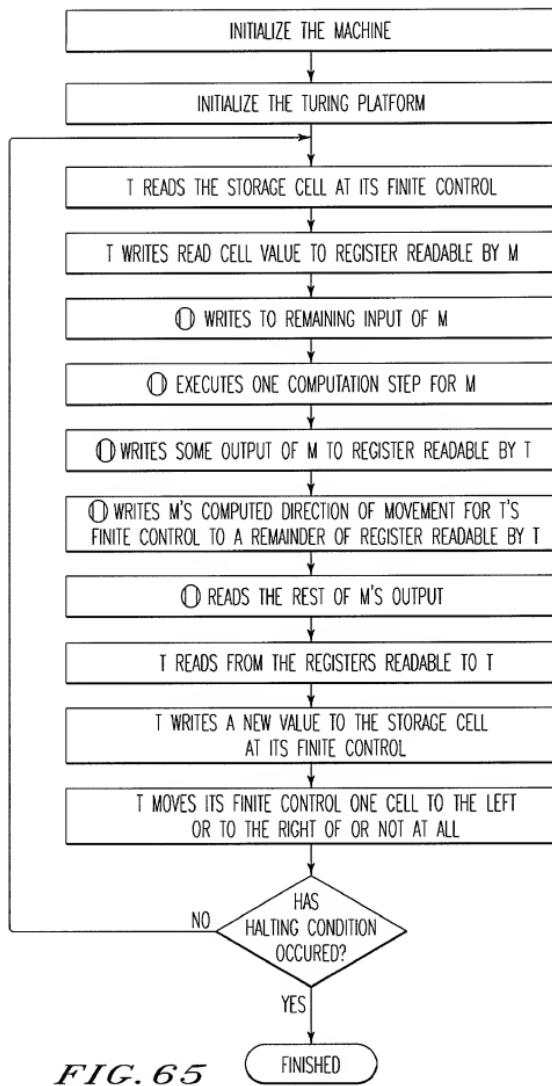


FIG. 65

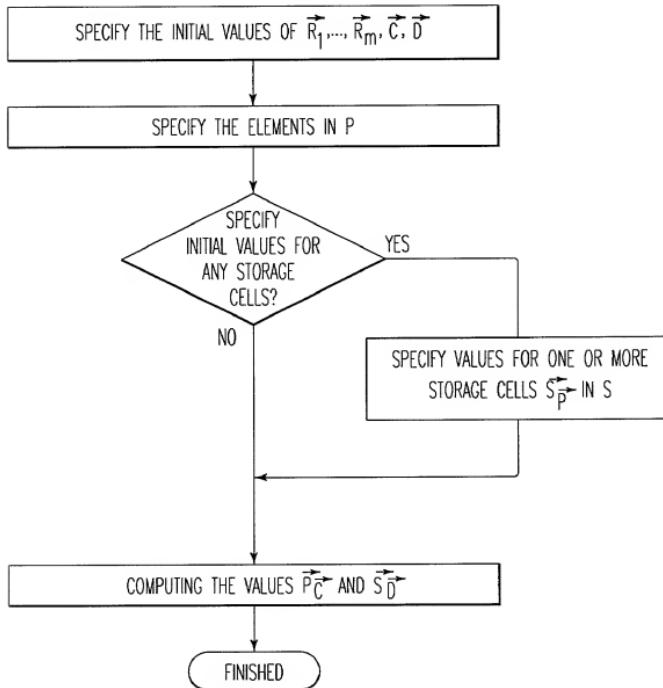


FIG. 66

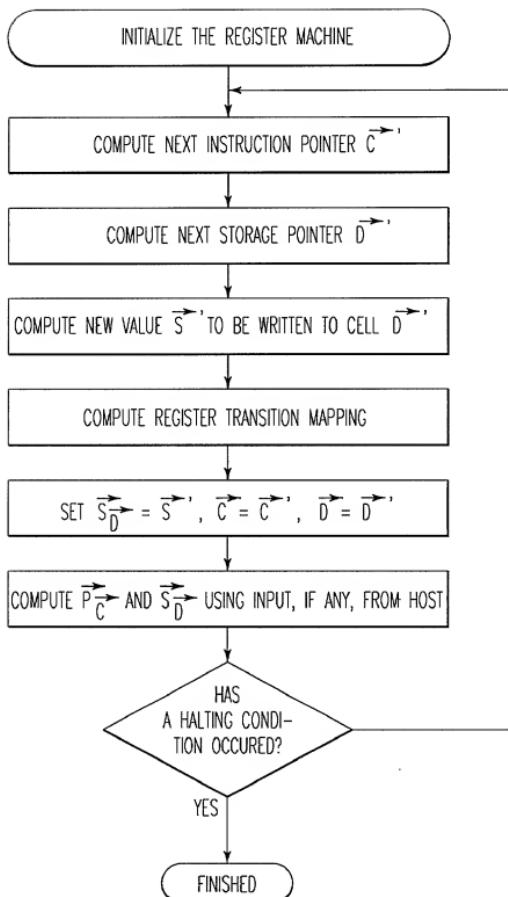
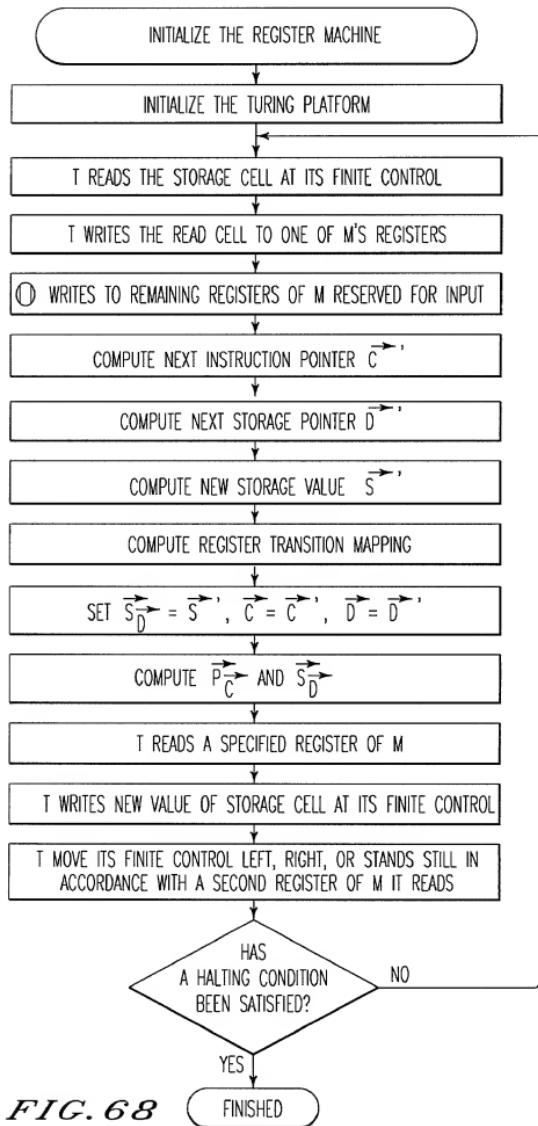


FIG. 67



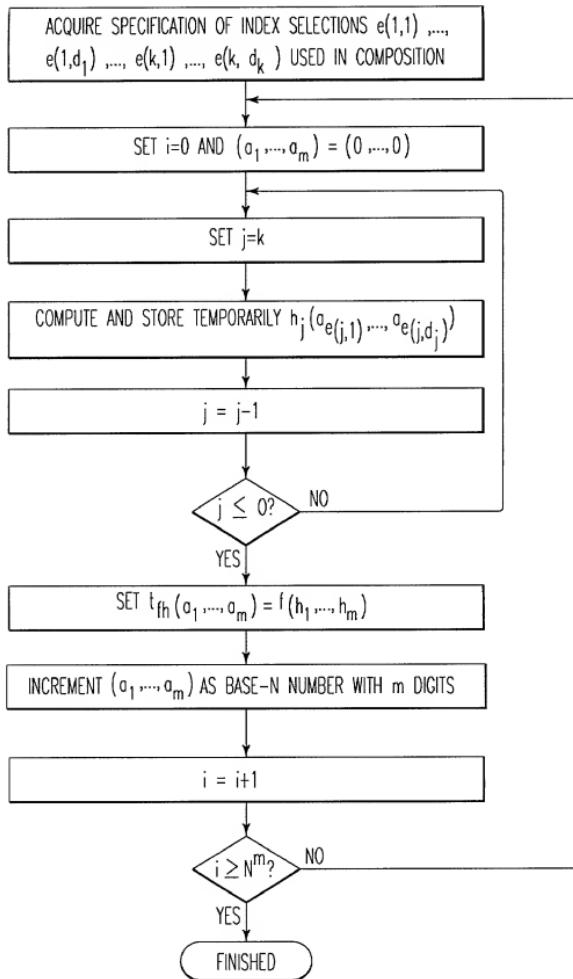


FIG. 69

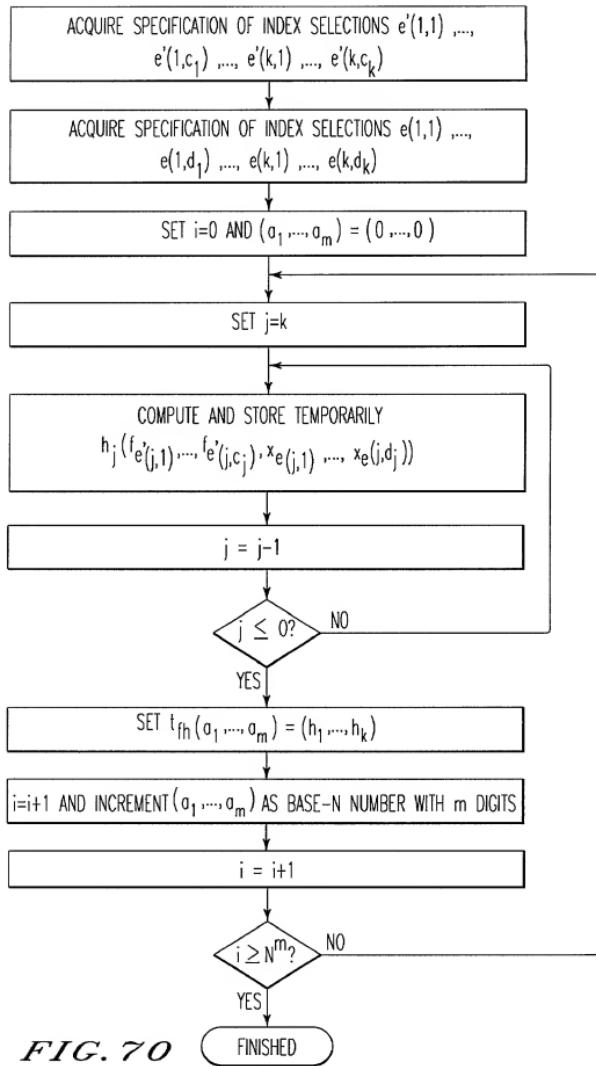


FIG. 70

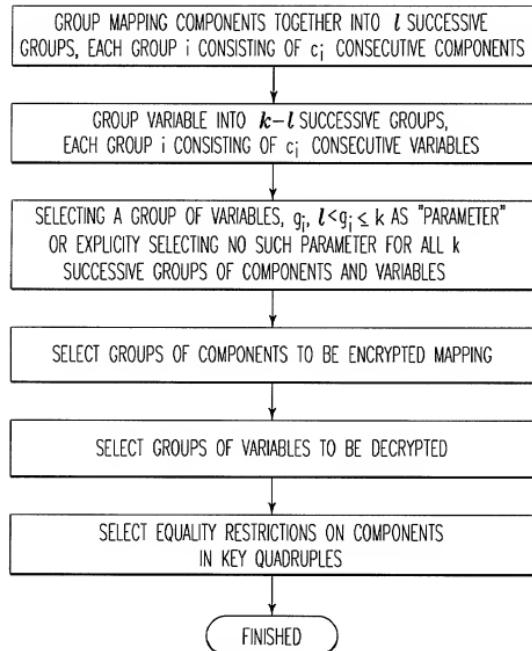
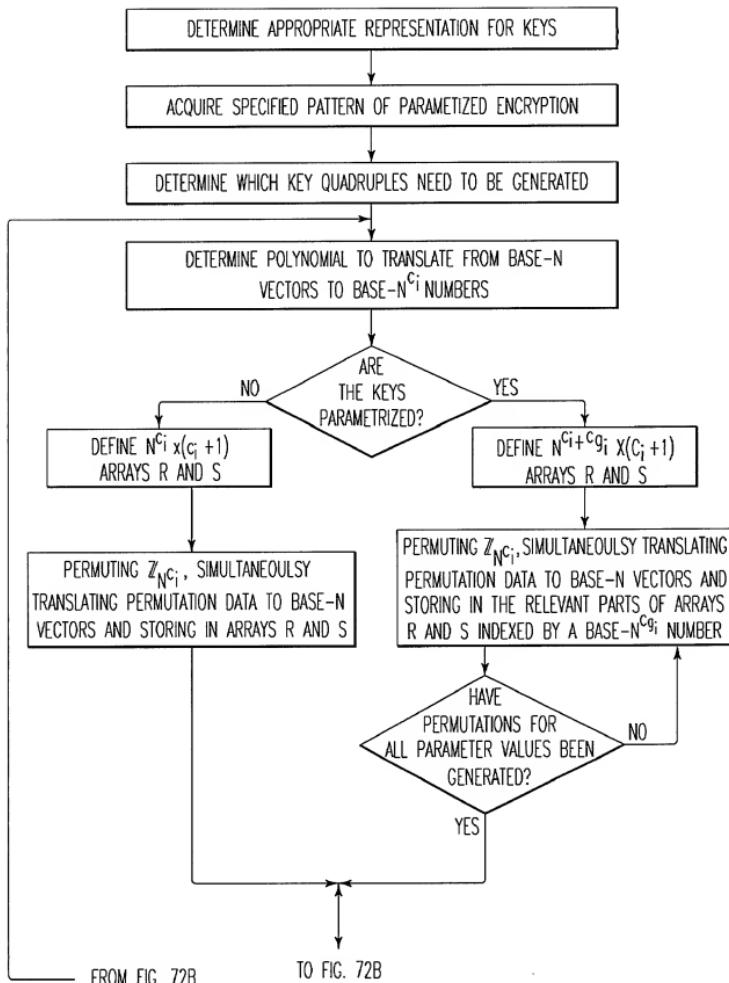


FIG. 71

**FIG. 72A**

TO FIG. 72A

FROM FIG. 72A

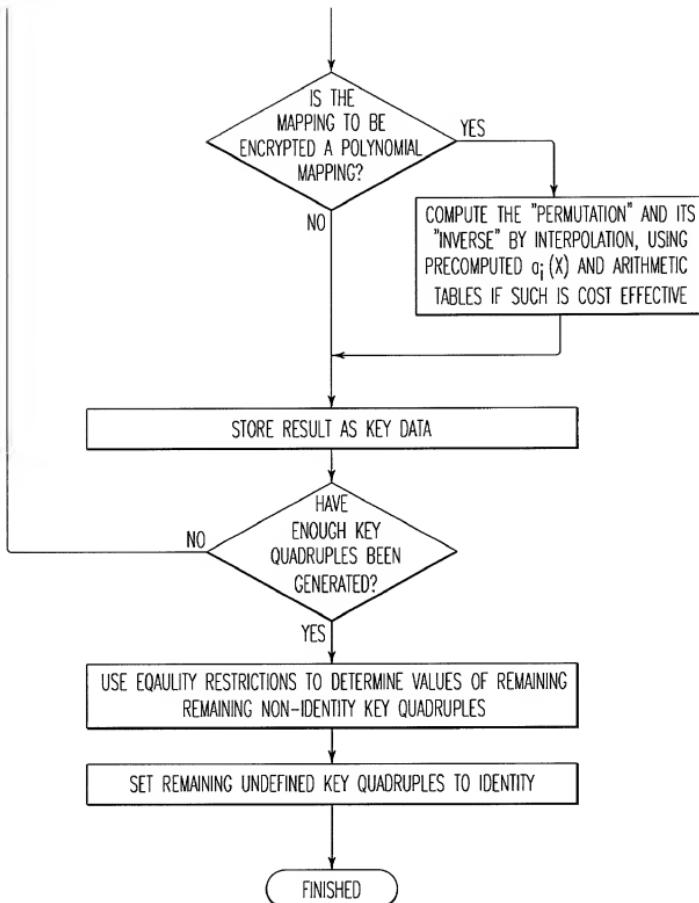


FIG. 72B

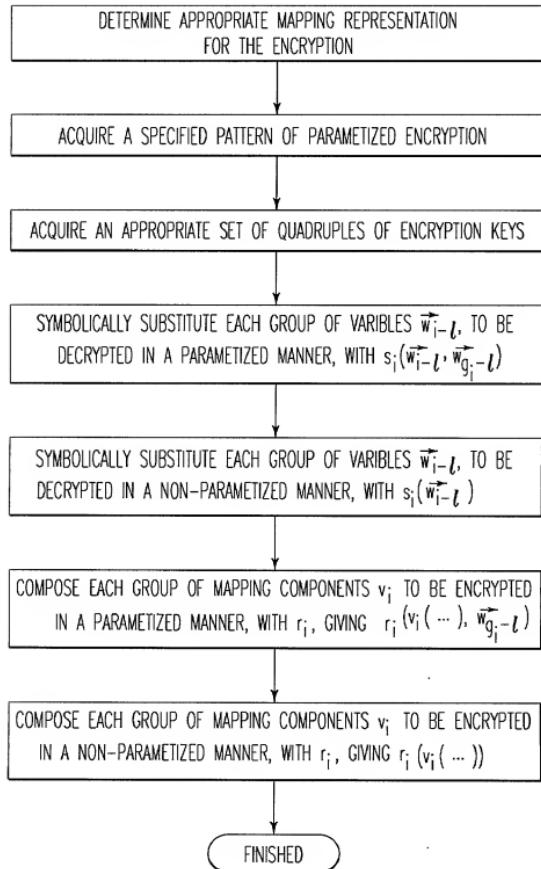
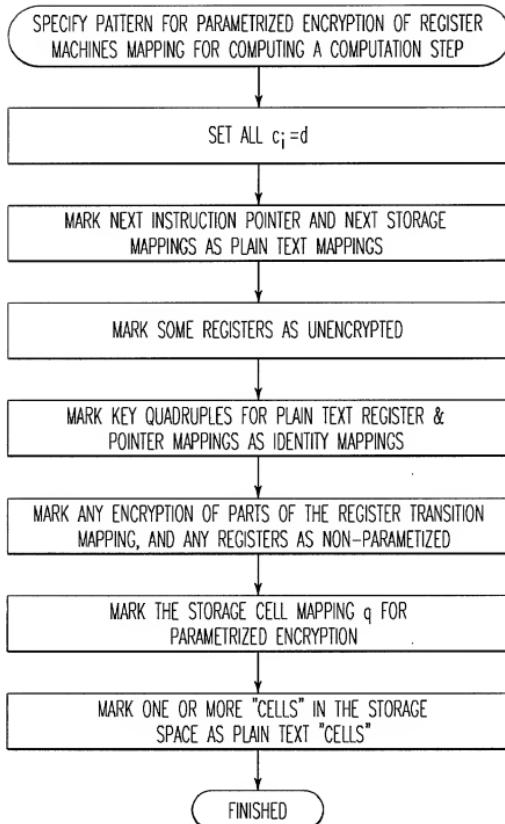


FIG. 73



**FIG. 74**

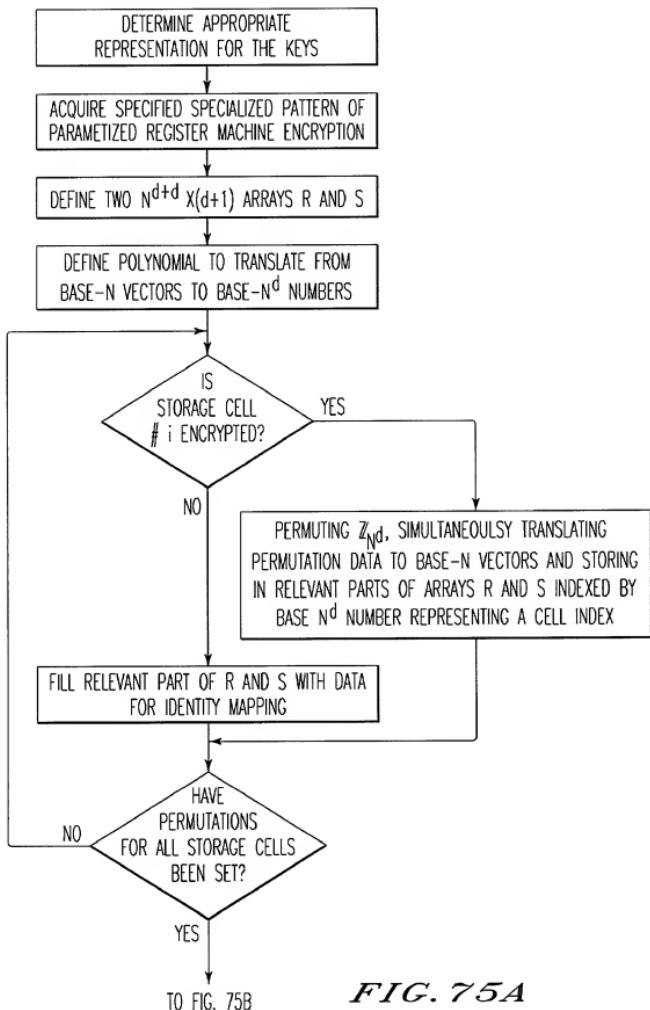
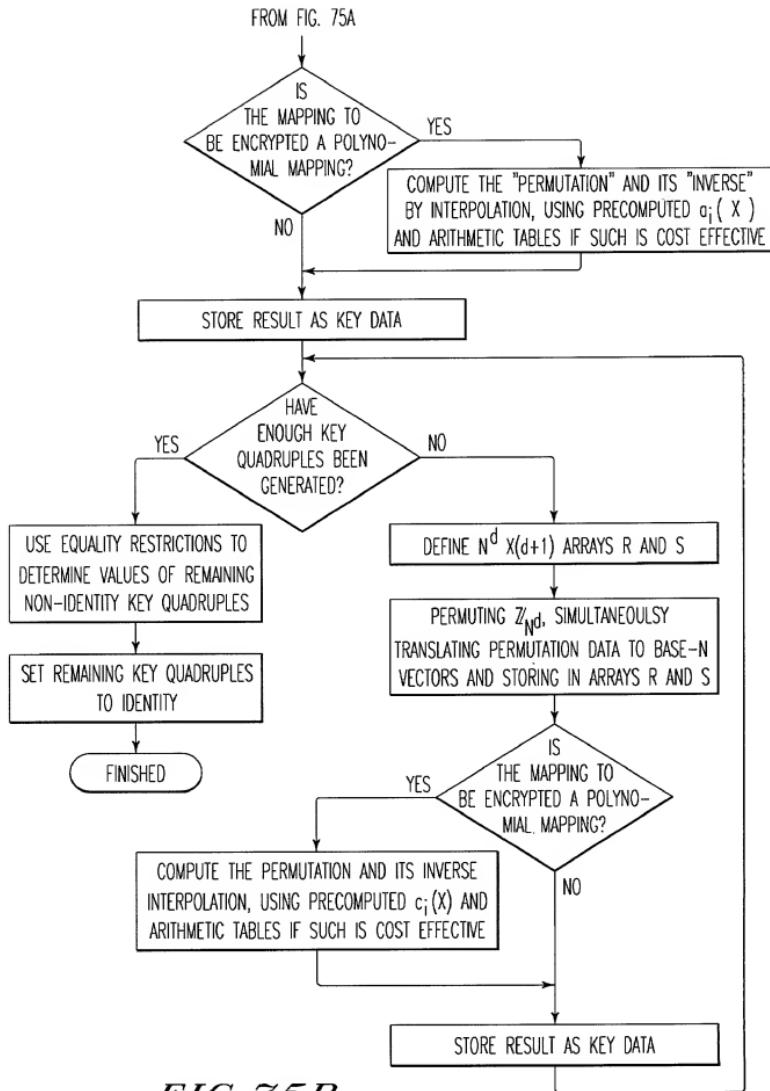
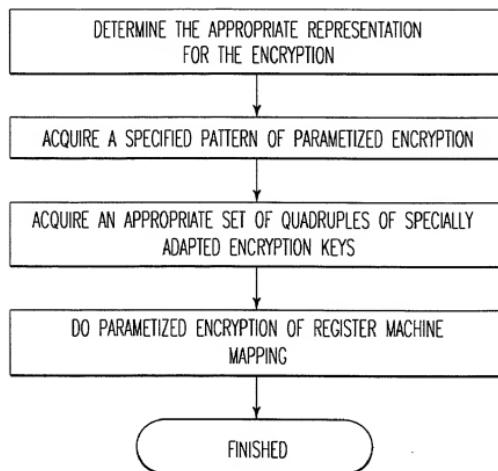


FIG. 75A

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*FIG. 76*